

# Assisted Partial Timing Support – Metrics

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Time in Distribution, Performance &  
Measurement

Kishan Shenoi ([kshenoi@Qulsar.com](mailto:kshenoi@Qulsar.com))

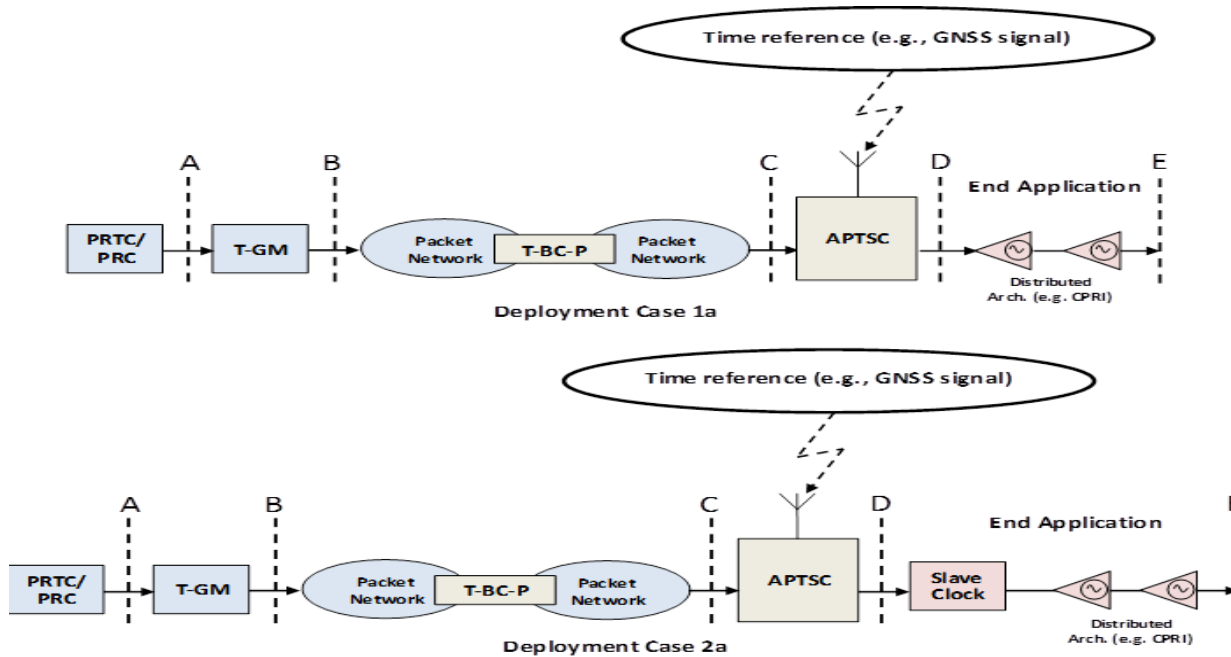
Qulsar, Inc., San Jose, California

# Outline

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- ▶ Principal concept of the Assisted “Partial-Support” approach for timing in a wireless (LTE) environment
  - ▶ Combination of GNSS and PTP approaches
- ▶ Mathematical principles underlying APTSC
  - ▶ Introduction to APTSC in companion presentation

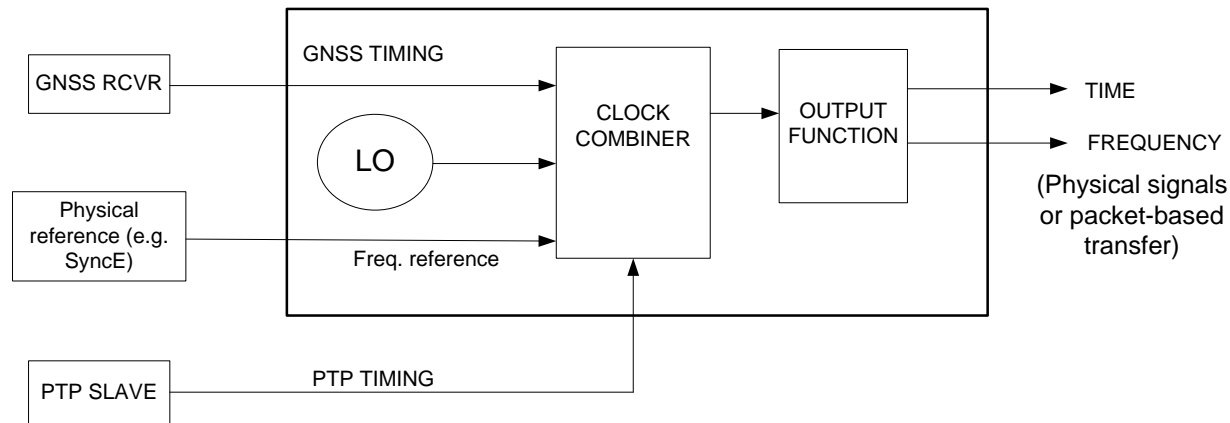
# Conceptual View of Assisted Partial-Support



(From ITU-T  
Contribution WD11-  
Copenhagen)

- ▶ The PRTC function is GNSS based (e.g. GPS)
- ▶ The packet network between device and upstream master (GM or T-BC) may not be full on-path support (hence “partial-support”)
- ▶ Primary reference for APTSC (and T-GM) is GNSS
- ▶ PTP provides time-holdover when GNSS becomes unavailable

# Conceptual View of APTSC



- ▶ Output function provides the output timing signal
  - ▶ PTP Master and/or 1PPS+ToD and/or frequency(e.g. 1544/2048)
- ▶ Clock Combiner considers all sources to generate the composite time/frequency to drive the output function
  - ▶ Primary reference GNSS
- ▶ Holdover (when GNSS is unavailable) using one or more of the other sources available
  - ▶ Physical references (e.g. SyncE may not be available)
- ▶ Not indicated: Ability to coordinate references (especially PTP and/or SyncE and/or GNSS working in concert)

# Operational Principles

## Primary Reference : GNSS

- ▶ While GNSS is active (“valid”):
  - ▶ Generate output clock (time/frequency) – time error < 100ns
    - ▶ Output time-clock absolute error should be < 100ns
  - ▶ Measure packet-delay variation (PDV) for PTP packets
  - ▶ Compute metrics that enable prediction of time-holdover when PTP used to generate output
  - ▶ Monitor performance of local oscillator and other references (if available)

## Secondary Reference : PTP

- ▶ When GNSS is lost (“invalid”):
  - ▶ Use PTP timing (frequency) to control progression of time-clock (case considered here)
    - ▶ Possible Alternative: use PTP time-clock (assuming asymmetry calibration)

## ▶ Tertiary Reference : LO / other Reference

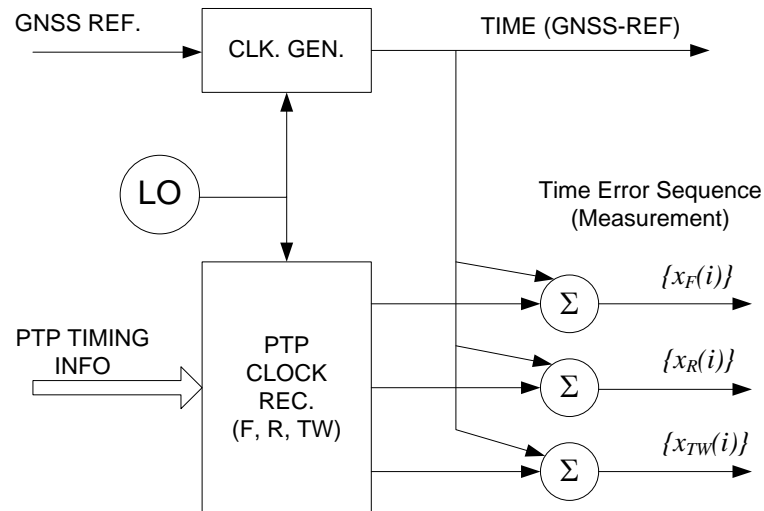
- ▶ Frequency reference/local-oscillator fallback if PTP timing is inadequate

# Mathematical Basis

- ▶ Let  $t = 0$  be the point that GNSS declared invalid. The time error of the “holdover clock” modeled as:

$$x(t) = x_0 + y_0 \cdot t + \underbrace{\int_0^t \gamma(\tau) d\tau + \varphi(t)}_{\text{Holdover error}}$$

- $x_0$  is the initial error (GNSS error + transient effect) (reduces holdover budget)
- $y_0$  is the initial frequency error (generally  $\approx 0$ )
- $\gamma(\ )$  is the frequency error due to temperature changes and aging
- $\varphi(\ )$  represents the random noise component
- Performance metrics computed on “holdover error” while GNSS valid to develop KPIs



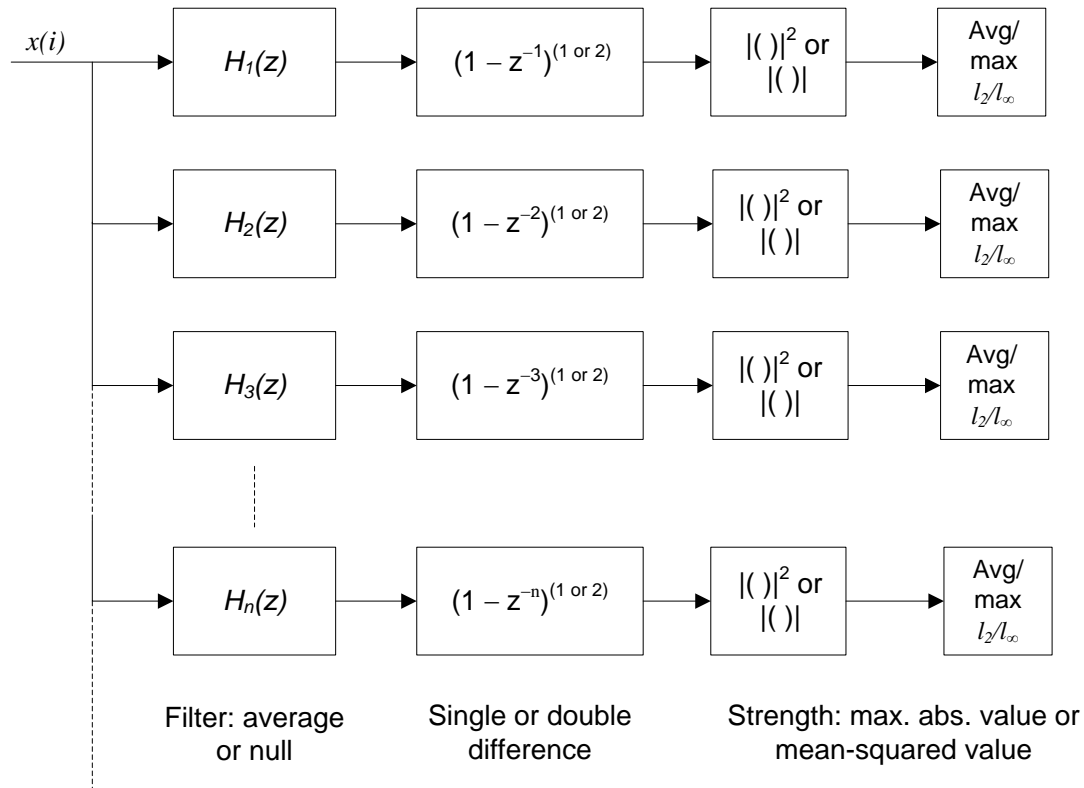
- ▶ PTP clock recovery could be based on one-way (F or R) or two-way
- ▶ The recovered PTP clock could be a physical signal or “paper clock”
- ▶ The PTP “clock recovery” processing block must include any non-linear operations such as packet selection
- ▶ The PTP “clock recovery” processing block may include linear-time-invariant operations such as low-pass filtering

# Metrics - Computation

- ▶ Metrics are computed on time error sequence  $\{x(k)\}$ ; implied sampling interval =  $\tau_0$
- ▶ Intent is to see how much dispersion could occur in an interval (*aka* observation interval)  $\tau = n\tau_0$
- ▶ *First difference* :  $\{x(k+n) - x(k)\}$  removes constant time error  $x_0$
- ▶ *Double difference* :  $\{x(k+2n) - 2x(k+n) + x(k)\}$  removes  $x_0$  as well as frequency offset  $y_0$
- ▶ *Smoothing function* (optional) : Average over  $n$  consecutive values
- ▶ *Strength calculation*: maximum-absolute value or mean-square value (variance) (square-root gives rms or standard deviation)



# Metrics - Computation



$$H_n(z) = \frac{1}{n} \cdot \sum_{k=0}^{n-1} z^{-k}$$

(average over n consecutive values)

- ▶ MTIE calculation does not fit neatly into this model
- ▶ Boundary points need to be handled with care when data set is finite

# Important Metrics

Metric	Strength calc.	Filter	Difference level	Comments
MATIE (MAFE)	maximum	averaging	First difference	Identifies frequency offset
TIE <sub>rms</sub>	(root) mean-square	none	First difference	Power of time error
TEDEV (TEVAR)	(root) mean-square	averaging	First difference	Power of time error
TDEV (TVAR)	(root) mean-square	averaging	Second difference	Power of time error
ADEV (AVAR)	(root) mean-square	none	Second difference	Power of time error (indirect)
MDEV (MVAR)	(root) mean-square	averaging	Second difference	Power of time error (indirect)

optimum prediction of time dispersion is proportional to ADEV:

$$\Delta t(\tau) = \text{constant} \cdot \tau \cdot \sigma_y(\tau)$$

# Example of Performance Estimation

- ▶ Assume:
  - ▶ Overall time-holdover requirement:  $1.5\mu\text{s}$
  - ▶ Budget for GNSS error and switching transient:  $500\text{ns}$
  - ▶ Holdover using PTP frequency recovery using master-slave direction (*sync\_messages*)
    - ▶ Packet rate: 32 pps
    - ▶ Selection mechanism: 1% over 100s windows
    - ▶ Filtering bandwidth: 1MHz
- ▶ One possible metric: MTIE
  - ▶ Requirement:  $\text{MTIE}(\tau) < 1000\text{ns}$
- ▶ Simulation:
  - ▶ 5 GigE switches
  - ▶ Load : mean load = 60% ; standard deviation = 20%

# Simulation Example

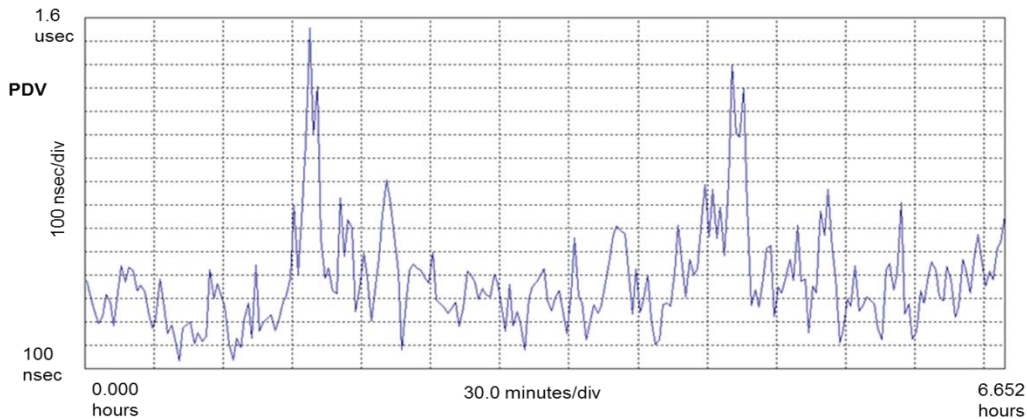
## ▶ Assumption:

- ▶ Overall time-holdover requirement:  $1.5\mu\text{s}$
- ▶ Budget for GNSS error and switching transient: 500ns
- ▶ Holdover using PTP frequency recovery using master-slave direction (*sync\_messages*)
  - ▶ Packet rate: 32 pps
  - ▶ Selection mechanism: 1% over 100s windows
  - ▶ Filtering bandwidth: 1mHz

## ▶ Simulation model:

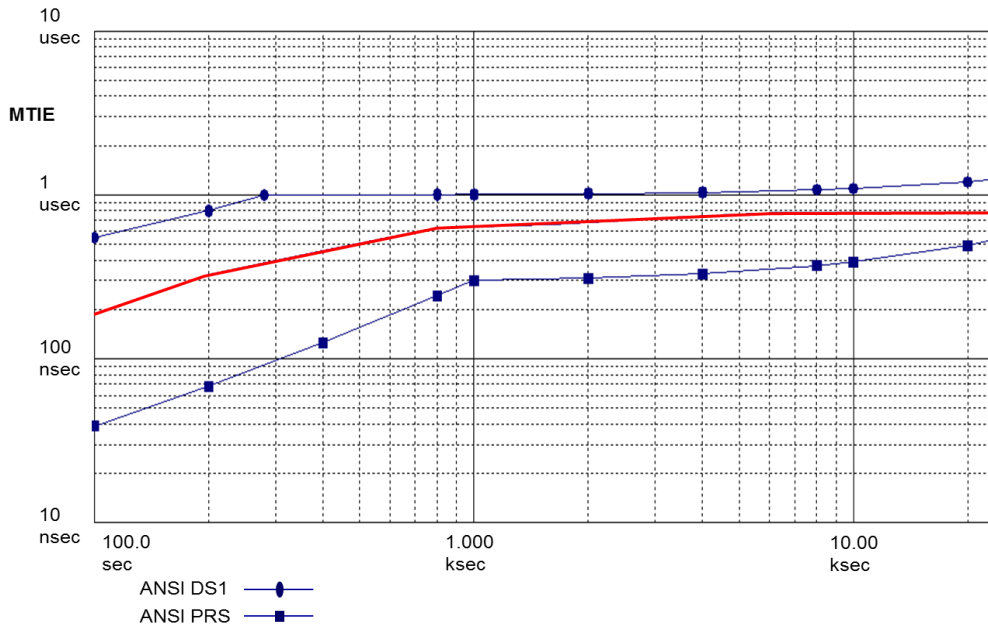
- ▶ PTP packet is “highest priority”
- ▶ Loading follows a flicker model, changing every 250ms
- ▶ Packet rate: 32pps
- ▶ PDV introduced in switch by “head-of-line blocking”
- ▶ Network has 5 GigE switches
- ▶ Interfering traffic... 90% is “large” packets (1.5kbyte)
- ▶ Load : mean load = 60% ; standard deviation = 20%

# Simulation Example



Packet-delay-variation (PDV)  
based on:

- “floor”
- 1-percentile
- 100s window
- representative transit delay equal 1-percentile average



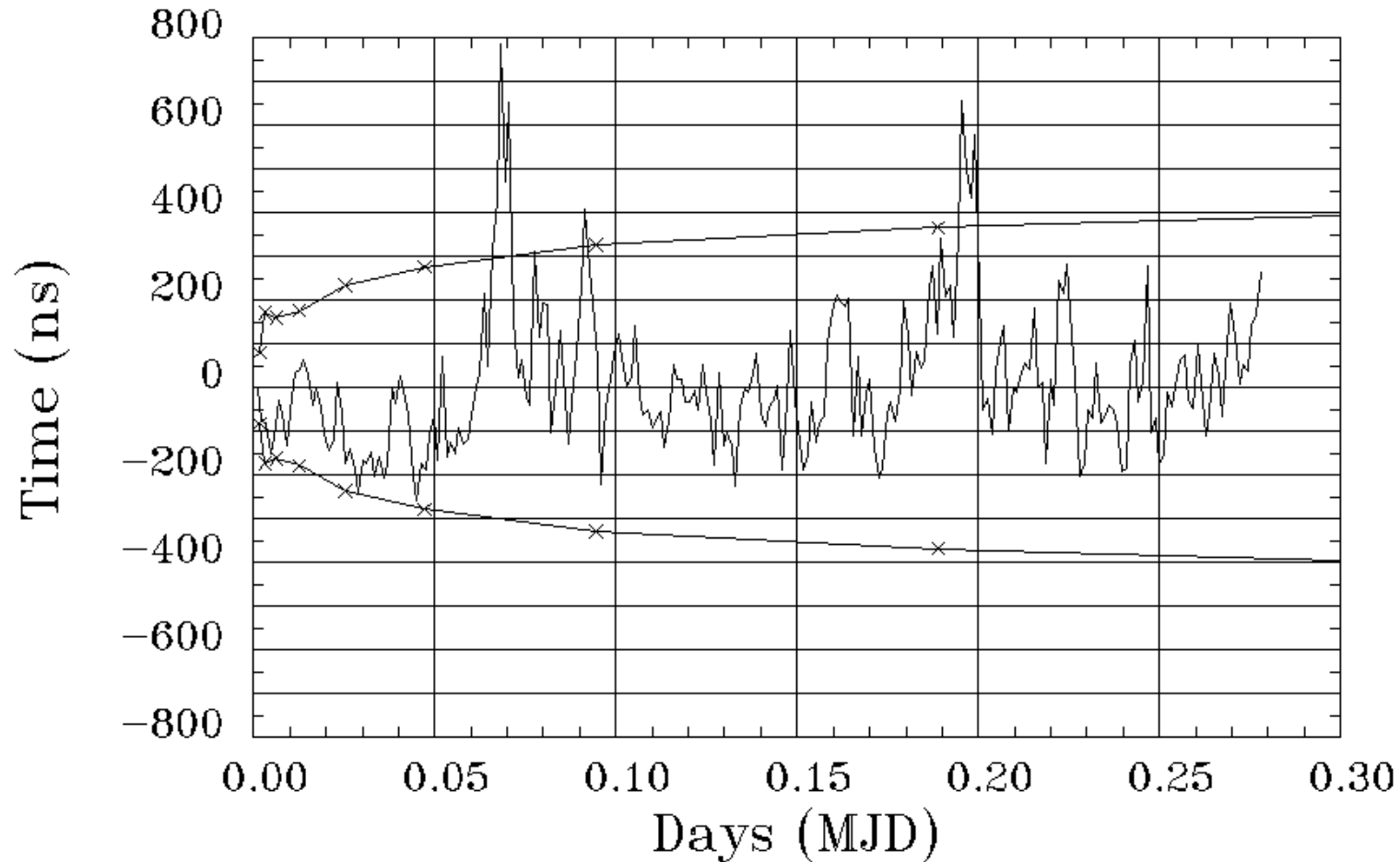
MTIE :

- 1MHz filter
- $< 1\mu\text{s}$

Conclusion:

- With this network PDV, PTP (one-way-frequency) can support time-holdover indefinitely
- “Alarm” condition: **GREEN**

## Expected Dispersion based on simulated PDV



Taken from earlier presentations by Dr. Marc Weiss

# Concluding Remarks

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- ▶ Time holdover using PTP can be predicted
- ▶ When GNSS is active the network PDV can be measured and quantified
  - ▶ Metrics are computed on measured PDV and not necessarily related to network configuration (such as number of switches)
- ▶ Metrics (e.g. MTIE, TDEV, etc.) quantify strength of noise process and estimates of (future) time dispersion if in holdover
- ▶ Companion presentation provides an introduction to the principles underlying Assisted Partial-Support

Thank You!

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Questions?

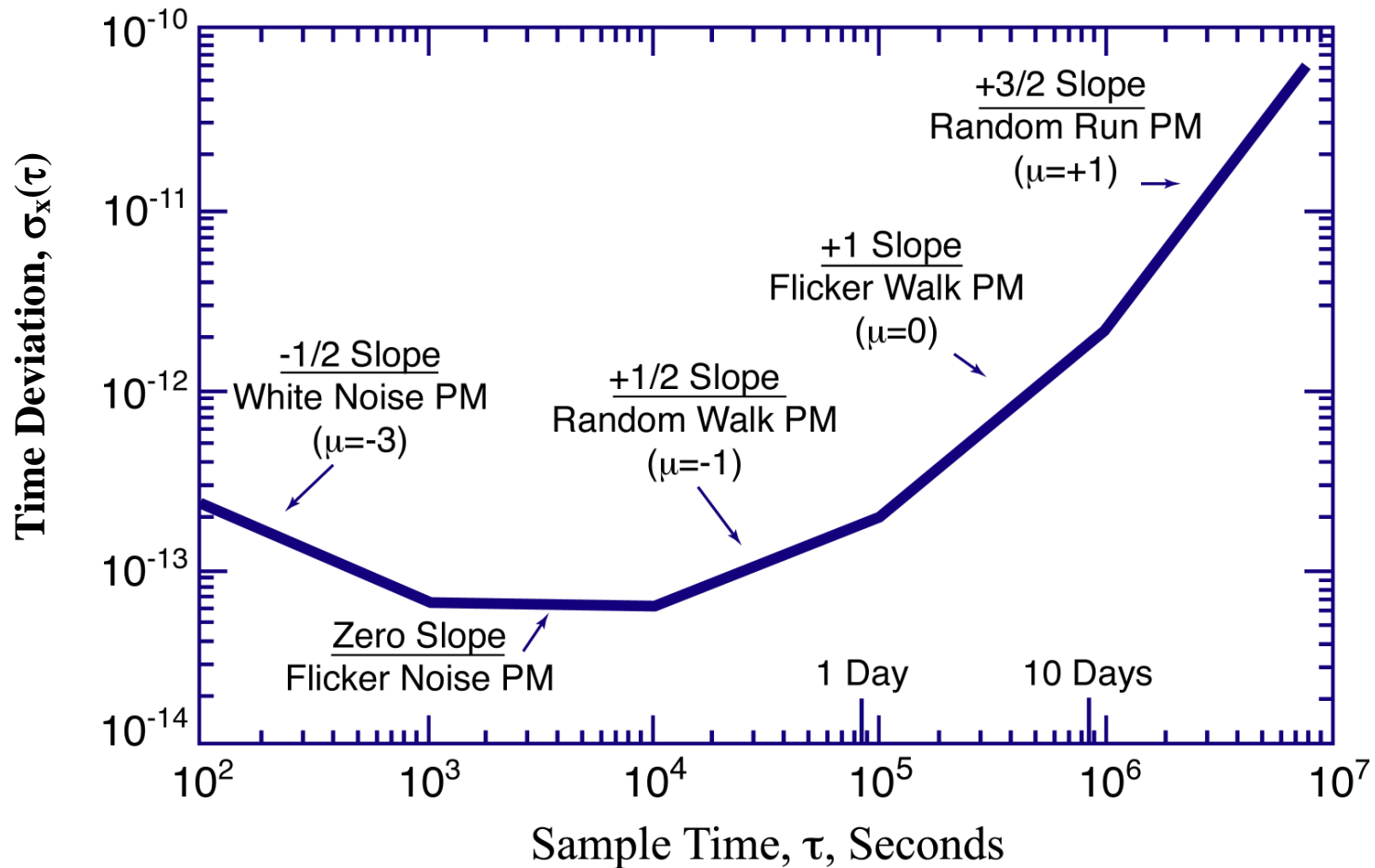
Kishan Shenoi (kshenoi@Qulsar.com)



# BACKUP SLIDES

# TDEV Reveals the Noise Type

## TIME STABILITY



Taken from earlier presentations by Dr. Marc Weiss

# Estimating Time Dispersion

Optimum Prediction is Based on Noise Types

$\alpha$	Typical Noise Types Name	Optimum Prediction $x(\tau_p)$ rms <sup>d</sup>	Time Error: Asymptotic Form
2	white-noise PM	$\tau_p \cdot \sigma_y(\tau_p) / \sqrt{3}$	constant
1	flicker-noise PM	$\sim \tau_p \cdot \sigma_y(\tau_p) \sqrt{\ln \tau_p / 2 \ln \tau_0}$	$\sqrt{\ln \tau_p}$
0	white-noise FM	$\tau_p \cdot \sigma_y(\tau_p)$	$\tau_p^{1/2}$
-1	flicker-noise FM	$\tau_p \cdot \sigma_y(\tau_p) / \sqrt{\ln 2}$	$\tau_p$
-2	random-walk FM	$\tau_p \cdot \sigma_y(\tau_p)$	$\tau_p^{3/2}$

<sup>d</sup> $\tau_p$  is the prediction interval.

These expressions are in terms of the Allan Deviation

Taken from earlier presentations by Dr. Marc Weiss