

Tutorial: Time and Time Error


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Presentation overview

- What is time?
- What is time error?
- Characterising time error

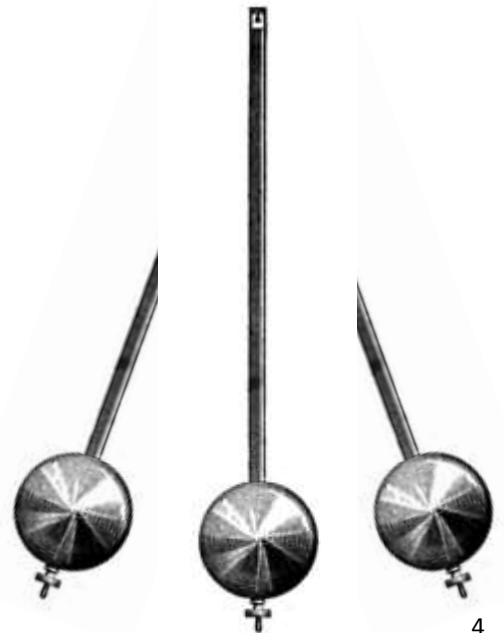
What is Time?

What is Time?

- Time is a fundamental physical dimension
 - Allows ordering and scheduling of events
 - Enables sharing of resources (e.g. time division multiplexing)
- Passage of time measured by counting a regularly repeating event
 - Astronomical events, e.g. day/night, month, year



- Physical events, e.g. pendulum, quartz resonance or atomic transitions



Common Time

- Common time requires a reference point
 - Time at an instant has no meaning without a reference
 - Need to start counting from a common point, or ***epoch***
 - Example: the Gregorian calendar counts years from the birth of Christ
- Legal and civil time based on UTC (Universal Time Co-ordinated)
 - Uses the Gregorian calendar epoch
 - Counts in step with TAI (atomic time)
 - Adjusted by leap seconds when required to match rotation of earth
 - Fixed offset added in each time zone to match daylight hours
- A ***time reference clock*** is a measurement device, counting at a constant frequency from a known epoch

Distributing Time

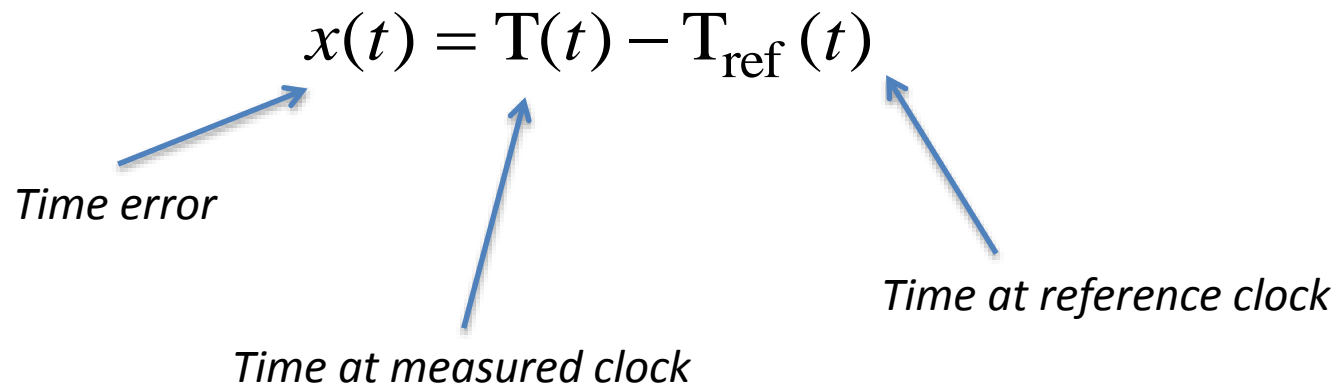


- Send a time message...
 - Need to know how long the message takes to get to the destination
 - A letter – might be usable for setting the date, e.g. next day delivery
 - A phone call – could use to set hour/minute/seconds, e.g. speaking clock
 - A packet – millisecond level accuracy
- GPS uses one-way messages
 - Uses knowledge of position and speed of light to estimate delay
- Send a return message
 - “Please check my time estimate”
 - Use round-trip delay to estimate one-way delay
 - Accuracy dependent on symmetrical delays
- Two way messaging used by both NTP and PTP

What is Time Error?

Time Error

- The ***time error*** of a clock is the difference between the time indicated by that clock and a reference clock
- Always relative: has no meaning without a reference
- Defined by ITU-T Recommendation G.810:

$$x(t) = T(t) - T_{\text{ref}}(t)$$


Time error

Time at measured clock

Time at reference clock

Direction of Time Error – clocks

Reference Clock:



Measured Clock:



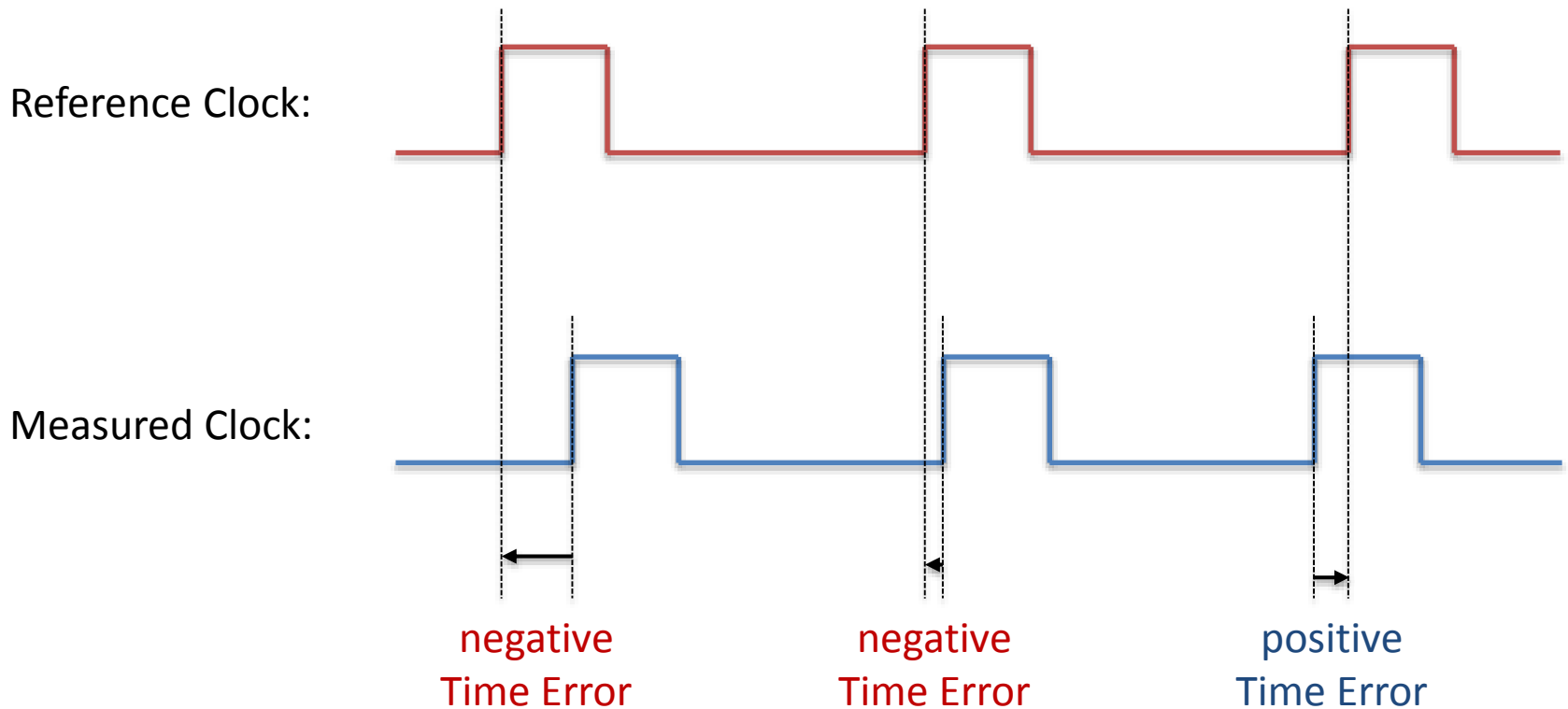
$$\begin{aligned} \text{Time Error} &= 11.55 - 12.00 \\ &= -5 \text{ minutes} \end{aligned}$$

$$\begin{aligned} \text{Time Error} &= 12.05 - 11.00 \\ &= +5 \text{ minutes} \end{aligned}$$

Clock lags reference (*slow, delayed*): **negative time error**

Clock leads reference (*fast, advanced*): **positive time error**

Direction of Time Error – signals



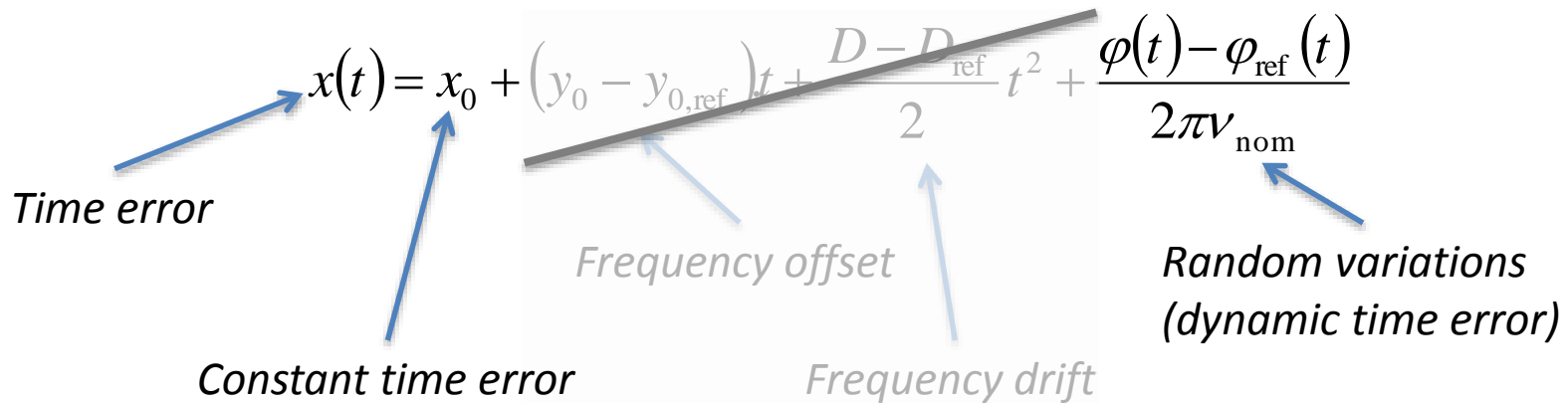
Signal lags reference (*slow, delayed*): **negative time error**

Signal leads reference (*fast, advanced*): **positive time error**

Characterising Time Error

Time Error Function

- Time error varies with time and can be expressed as a function:

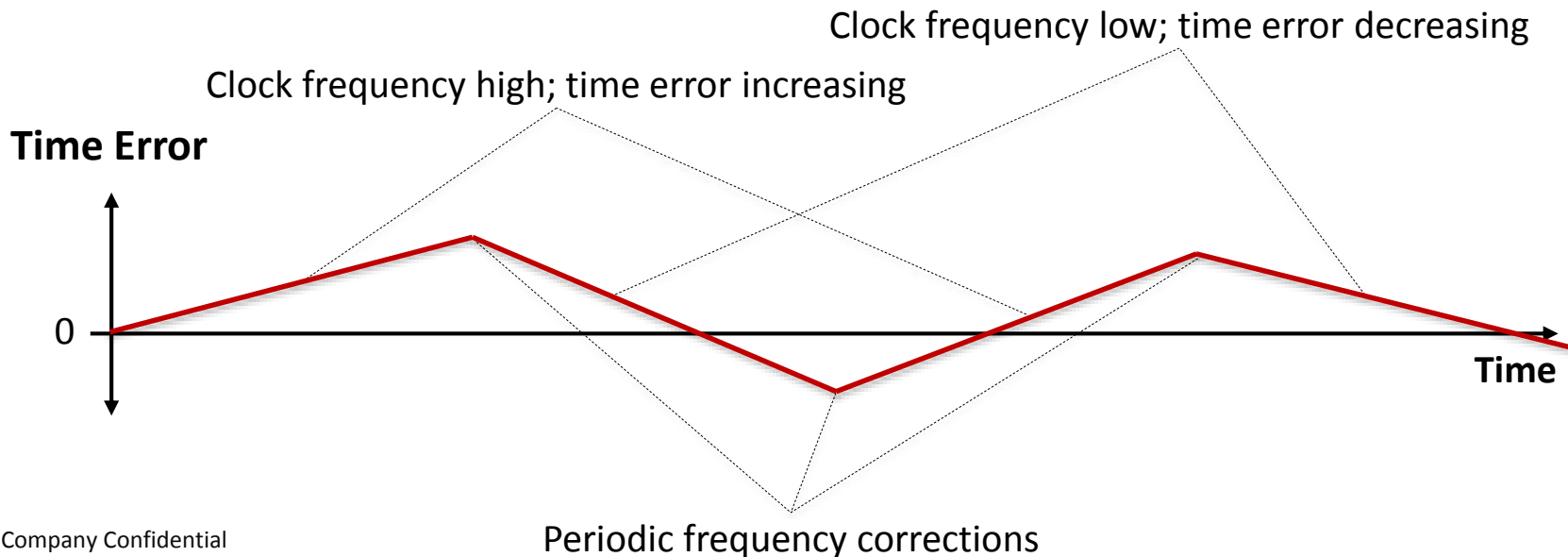
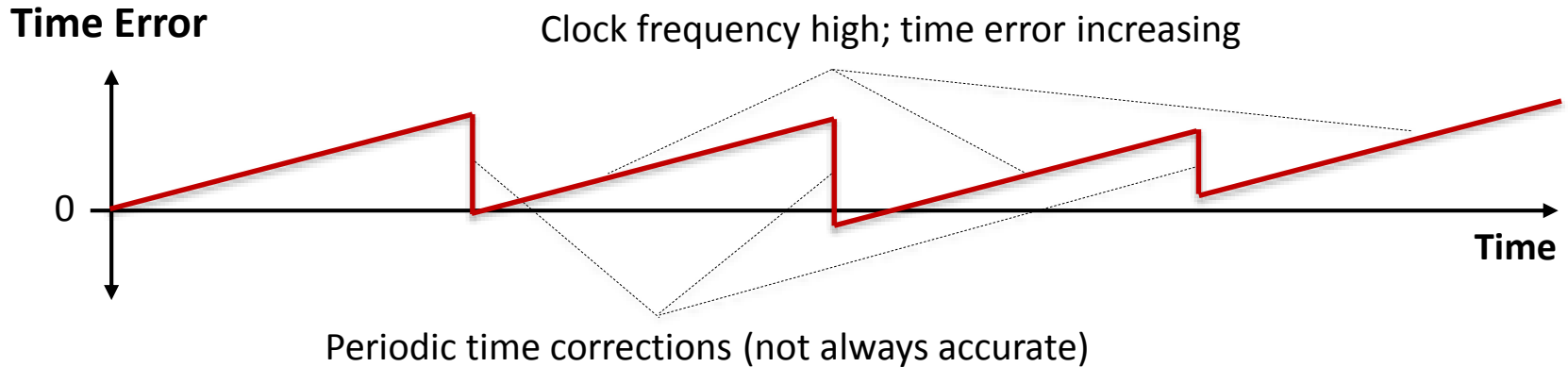
$$x(t) = x_0 + (y_0 - y_{0,\text{ref}})t + \frac{D - D_{\text{ref}}}{2}t^2 + \frac{\varphi(t) - \varphi_{\text{ref}}(t)}{2\pi\nu_{\text{nom}}}$$


The diagram shows the equation $x(t) = x_0 + (y_0 - y_{0,\text{ref}})t + \frac{D - D_{\text{ref}}}{2}t^2 + \frac{\varphi(t) - \varphi_{\text{ref}}(t)}{2\pi\nu_{\text{nom}}}$ with blue arrows pointing from descriptive labels to the corresponding terms in the equation:

- Time error** points to $x(t)$.
- Constant time error** points to x_0 .
- Frequency offset** points to $(y_0 - y_{0,\text{ref}})$.
- Frequency drift** points to $\frac{D - D_{\text{ref}}}{2}$.
- Random variations (dynamic time error)** points to $\frac{\varphi(t) - \varphi_{\text{ref}}(t)}{2\pi\nu_{\text{nom}}}$.

- If clocks are locked in phase, frequency offset and drift are eliminated, and time error reduces to two components:
 - Constant time error** or offset
 - Dynamic time error** or random variations

Examples of Time Error Functions



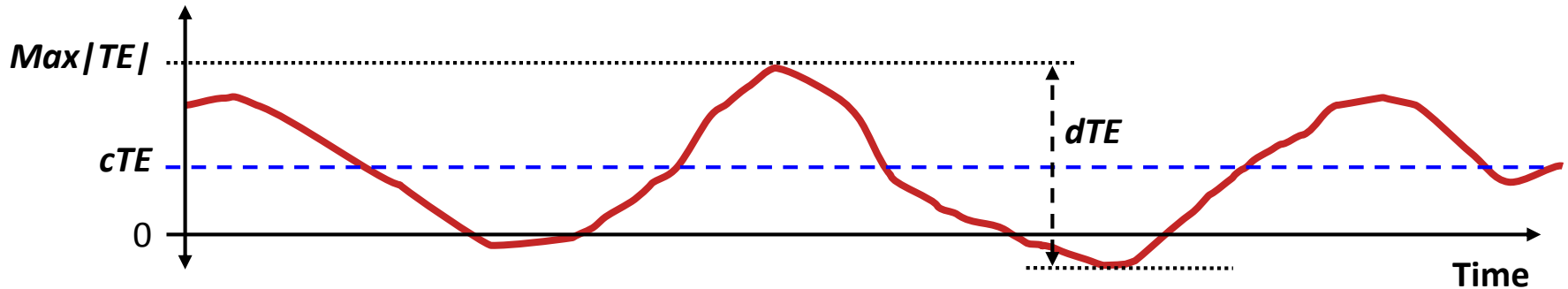
Measuring Time Error

- **Need an accurate time reference!**
 - Time has no meaning without a reference
- **Maximum Absolute Time Error ($Max|TE|$)** is the maximum distance from zero of the time error function
 - Sign doesn't matter: excursions may be positive or negative
- **Constant Time Error (cTE)** is the mean of the time error function
 - Period over which mean is measured is not specified; depends on signal
- **Dynamic Time Error (dTE)** is the change of the time error function
 - Effectively this is the phase or time wander
 - Analysed using MTIE and TDEV

Time Error and Time Interval Error (TIE)

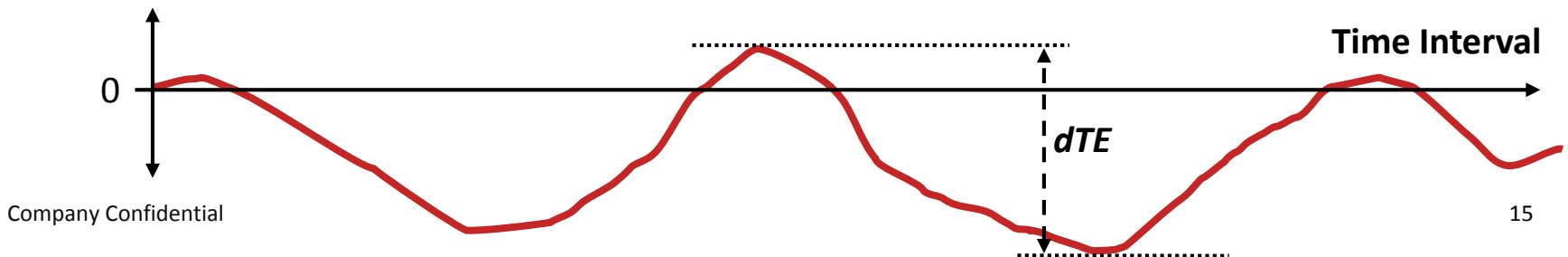
- Time Error measures the time difference between two clocks

Time Error



- Time Interval Error measures change of time error
 - Starts at zero, then tracks the change of time error (dTE)

Time Interval Error



Time Error Specifications

Time error limits may be specified for:

- Equipment clock wander or noise generation
 - e.g. PRTC, T-GM, T-BC, T-TSC
- Network limits at reference points
 - e.g. output of T-GM, output of network, output of end equipment

Time error specified using a combination of three parameters:

- Max Absolute Time Error (**max|TE|**) - specified in nanoseconds
- Constant Time Error (**cTE**) - specified in nanoseconds
- Dynamic Time Error (**dTE**) - specified with MTIE & TDEV masks

Not all parameters may be specified

- Network limit at output of network only specifies max|TE| and dTE
- Noise generation of a T-BC specifies max|TE|, cTE and dTE

INTEGRITY

TIME ERROR MEASUREMENTS REQUIRE TRUE PRECISION

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