

# Time and Frequency Measurements in Synchronization and Packet Networks

ITSF 2009  
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- ▶ Introduction
  - Synchronization “TIE” vs. packet “PDV” measurements
  - Measurement equipment overview
- ▶ Synchronization Measurements
  - Measuring TIE
  - Analysis from TIE
- ▶ Packet Metrics
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  - Frequency transport metrics
  - Time transport metrics
- ▶ Case Studies
  - Asymmetry in microwave, SHDSL, wireless backhaul
  - Metro Ethernet network
  - National Ethernet network

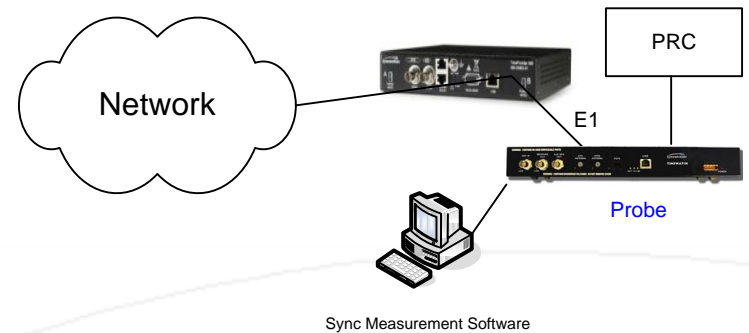
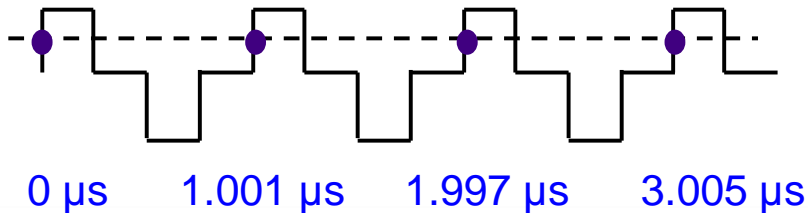
- ▶ “TIE” vs “PDV”
  - Traditional TDM synchronization measurements: signal edges are timestamped producing a sequence of samples
  - Packet timing measurements: packet departure/arrival times are sampled and packet delay sequences are formed
  - Both require (1) PRC/GPS; (2) Precision HW timestamping; (3) PC + SW
  
- ▶ Phase measurements (TIE) can be made using:
  - Frequency/time interval counters
  - Time interval analyzers
  - Dedicated test-sets
  - BITS/SSU clocks with built-in measurement capability
  - GPS receivers with built-in measurement capability
  
- ▶ Packet phase measurements (PDV) can be made using:
  - IEEE 1588 grandmaster/probes
  - NTP servers/probes
  - Specialized network probes

# “TIE” vs. “PDV”



## ► “TIE” (Single Point Measurement)

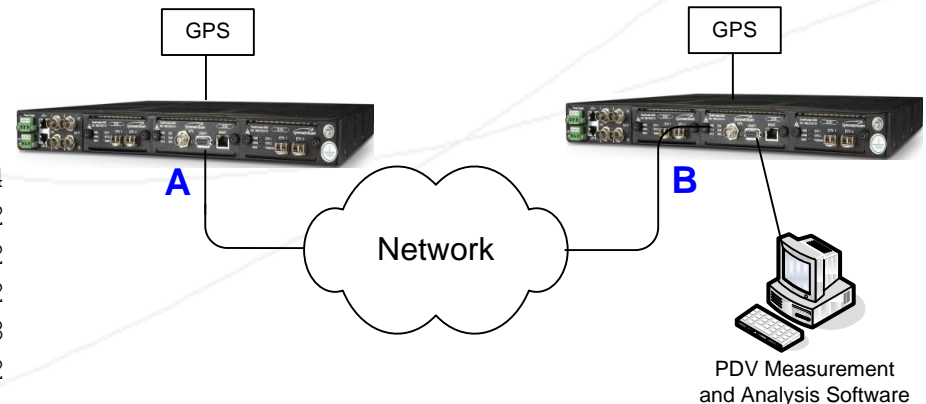
- Measurements are made at a single point – a single piece of equipment in a single location - a phase detector with reference - is needed



## ► “PDV” (Dual Point Measurement)

- Measurements are constructed from packets time-stamped at two points – in general two pieces of equipment, each with a reference, at two different locations – are needed

|   | Timestamp A          | Timestamp B          |
|---|----------------------|----------------------|
| F | 1233166476.991204496 | 1233166476.991389744 |
| R | 1233166476.980521740 | 1233166476.980352932 |
| F | 1233166477.006829496 | 1233166477.007014512 |
| R | 1233166476.996147084 | 1233166476.995977932 |
| F | 1233166477.022454496 | 1233166477.022639568 |
| R | 1233166477.011771820 | 1233166477.011602932 |

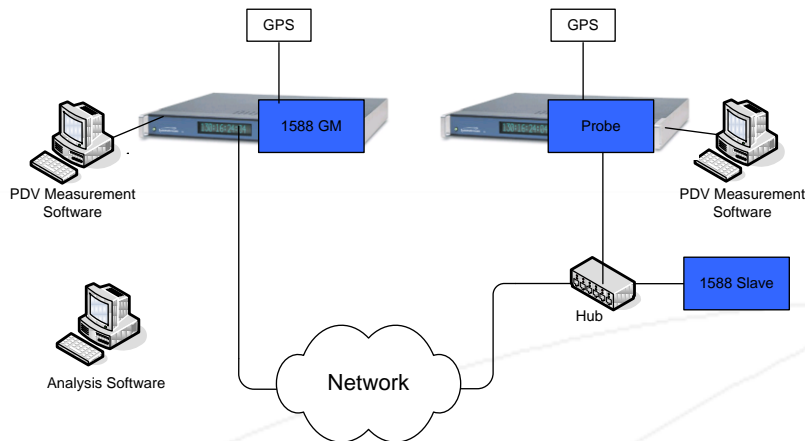


# “PDV” Measurement Setup Options



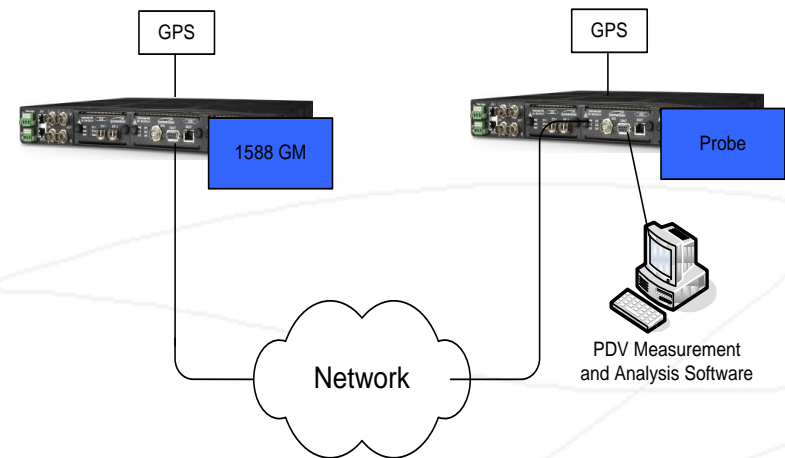
## Passive Probe

- (1) Hub or Ethernet Tap
- (2) IEEE 1588 Slave
- (3) Collection at Both Nodes



## Active Probe

- (1) No Hub or Ethernet Tap Needed
- (2) No IEEE 1588 Slave Needed
- (3) Collection at Probe Node Only



## “PDV”

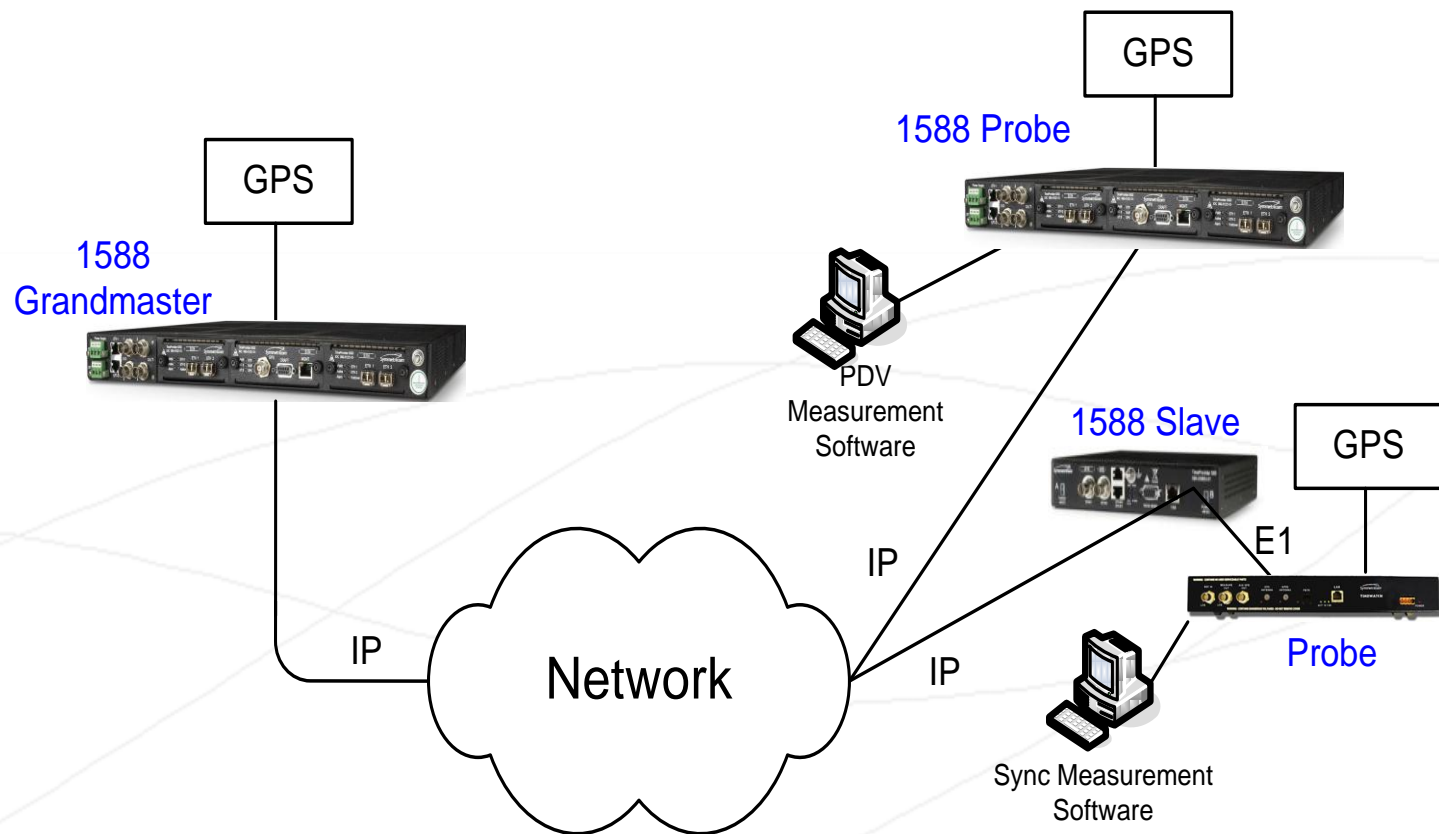
- Ideal setup - two packet timestampers with GPS reference so absolute latency can be measured as well as PDV over small to large areas
- Alternative setup (lab) – frequency (or GPS) locked single shelf with two packet timestampers
- Alternative setup (field) – frequency locked packet timestampers – PDV but not latency can be measured

- ▶ Are “TIE” Measurements still important? Yes!
  - Needed for the characterization of packet servo slaves such as IEEE 1588 slave devices
  - There are still oscillators and synchronization interfaces to characterize
  - “TIE” measurement/analysis background important to the understanding of “PDV” measurement/analysis
  - Many of the tools can be applied to either “TIE” or “PDV” data such as TDEV or spectral analysis
  - But there are new tools and new approaches to be applied to “PDV” with some of the traditional “TIE” tools less effective for “PDV” analysis

# “TIE” and “PDV”



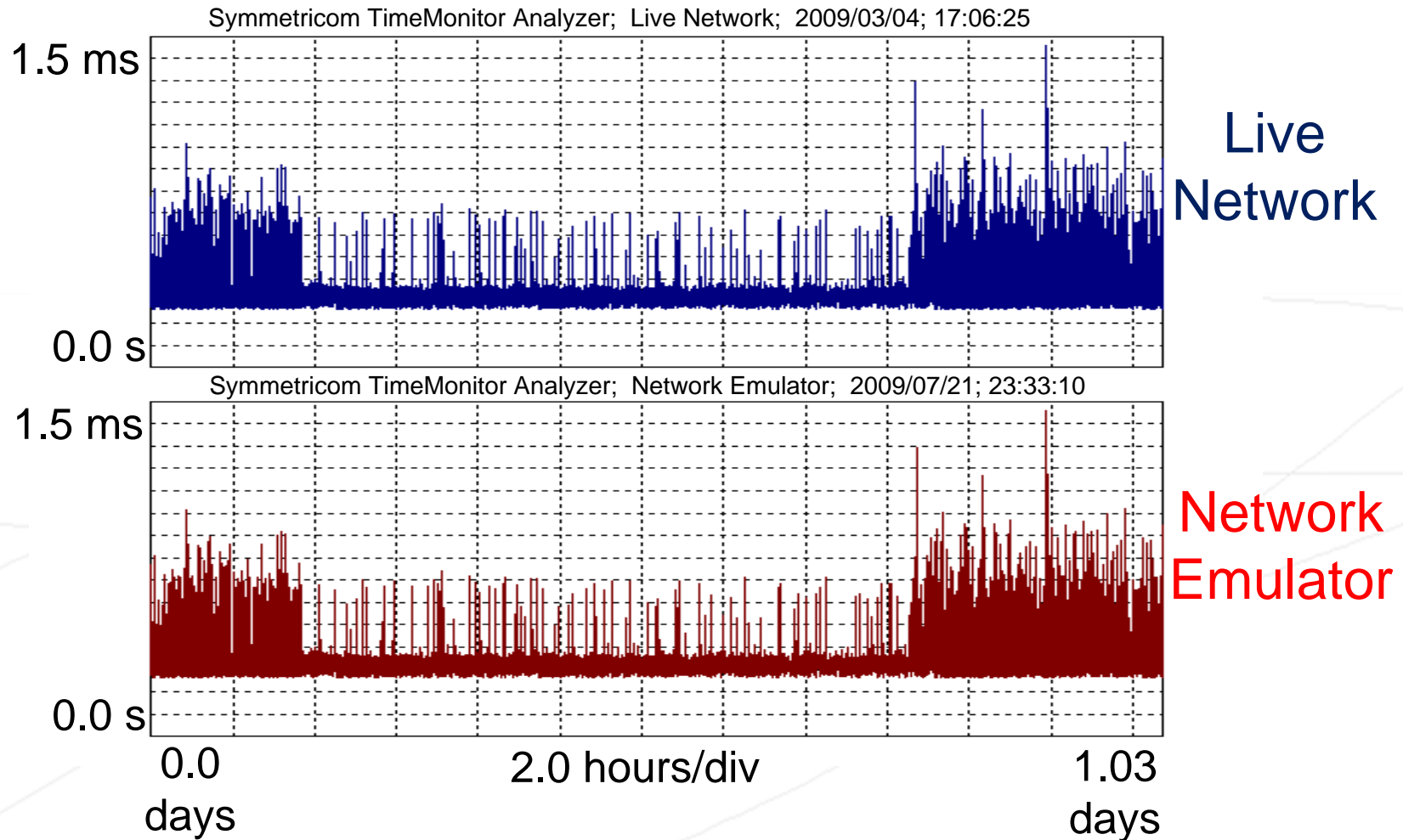
In most packet network measurement setups, both “TIE” and “PDV” are measured at the same time



# PDV Measurement Equipment Complement: Network Emulator



## Network Emulator

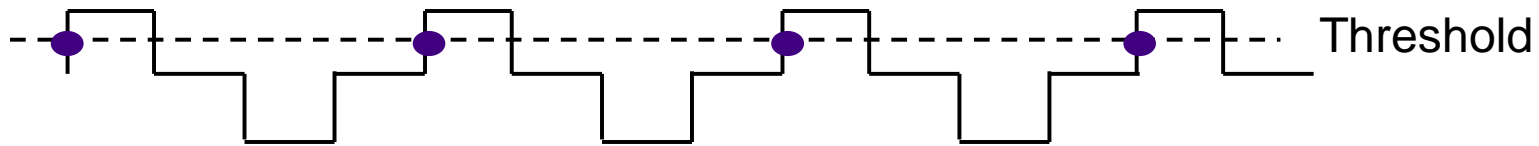




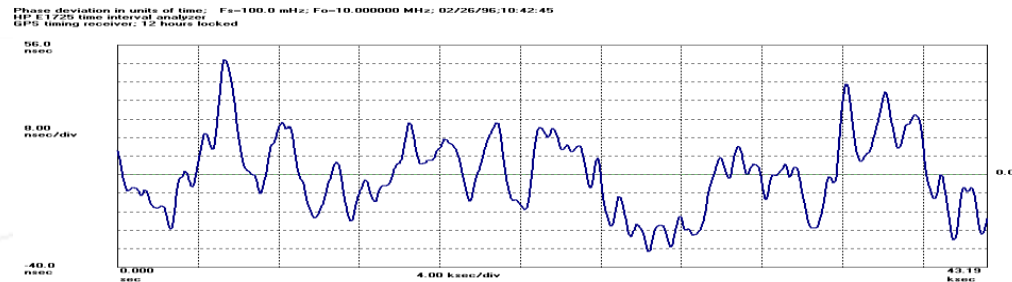
# TIE Measurement and Analysis: 3 step process



## 1. Timestamps

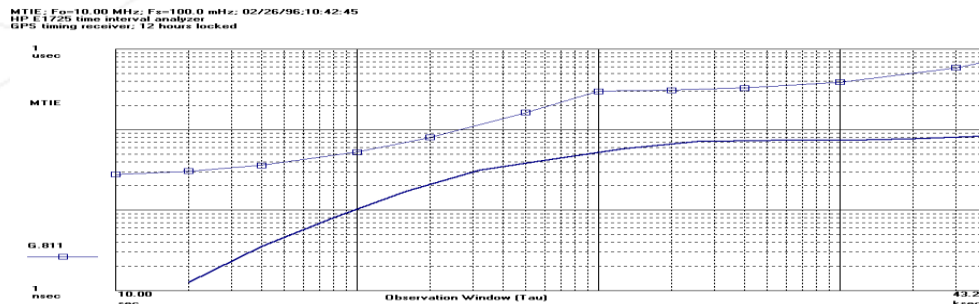


## 2. Phase



Phase Deviation  
or TIE

## 3. Analysis



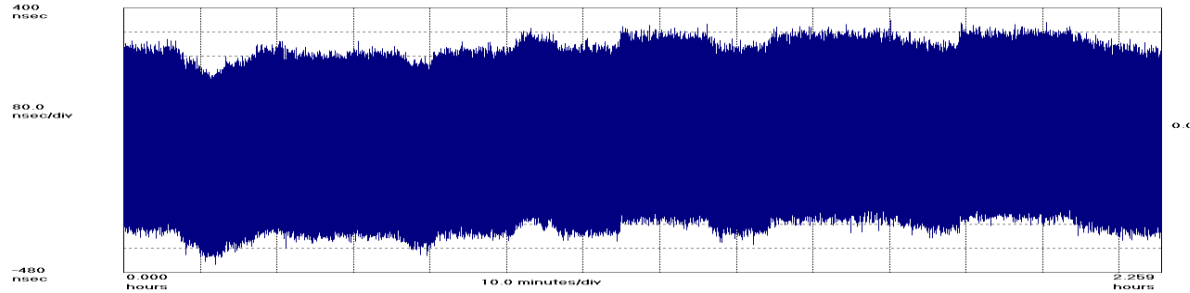
MTIE, TDEV,  
Allan Variance,  
Frequency, PPSD,  
etc.

1. **Analysis:** Frequency/MTIE/TDEV etc. derived from phase
2. **Check:** Verify measurement is properly made
  - Sudden (point-to-point) large movements of phase are suspect. For example, if MTIE fails the mask, it could be a measurement problem. Phase will help to investigate this.
  - Large frequency offset is easily seen: Is the reference OK? Is the equipment set to use the external reference?
3. **Timeline:** The processed measurements don't show what happened over time. Is the measurement worse during peak traffic times? Is the measurement worse in the middle of the night during maintenance activities?

# Analysis from Phase: Jitter & Wander

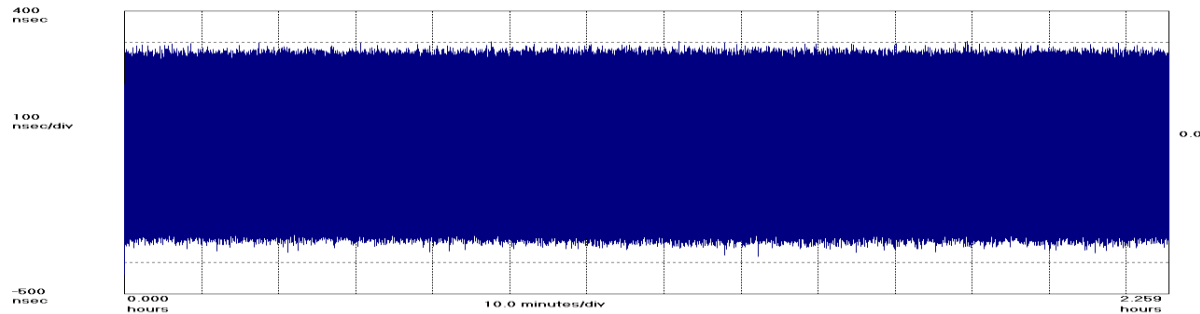


Symmetricom TimeMonitor Analyzer  
Phase deviation in units of time: Fs=31.48 Hz; Fo=2.0480000 MHz; 01/16/98; 10:58:04  
No filter



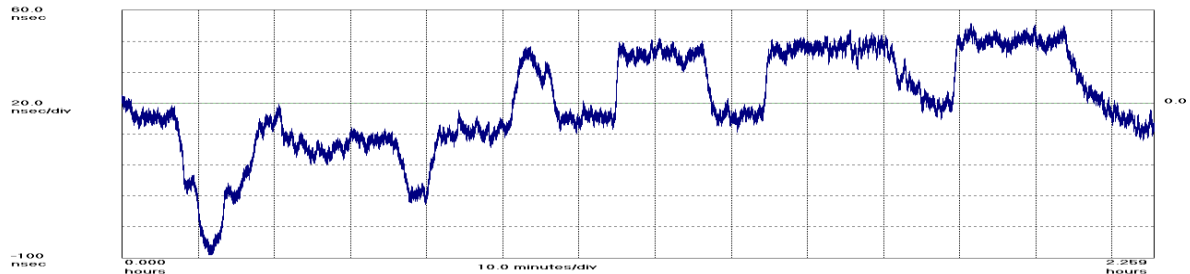
Signal (no filter)

Symmetricom TimeMonitor Analyzer  
Phase deviation in units of time: Fs=31.48 Hz; Fo=2.0480000 MHz; 01/16/98; 10:58:04  
Jitter: high-pass filter applied



Jitter (high-pass filter)  
1.52 UI peak-to-peak (E1)

Symmetricom TimeMonitor Analyzer  
Phase deviation in units of time: Fs=31.48 Hz; Fo=2.0480000 MHz; 01/16/98; 10:58:04  
Wander: low-pass filter applied



Wander (low-pass filter)

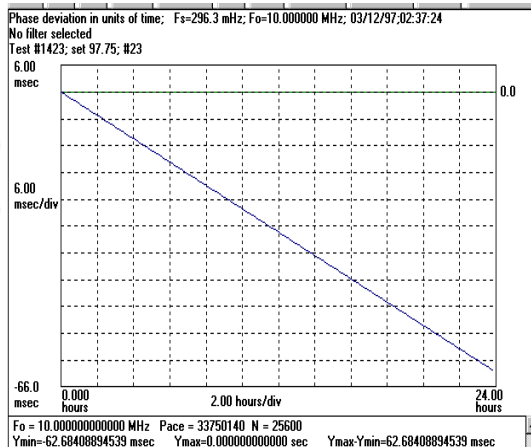
# Analysis from Phase: Frequency



- Recall the relationship between frequency and phase:

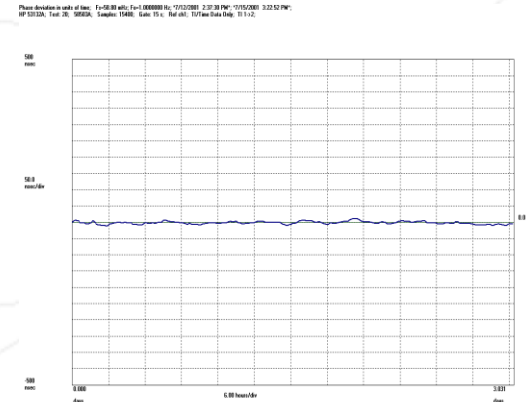
$$\omega = \frac{d\phi}{dt}$$

- Important point: Frequency is the slope in the phase plot



← Frequency offset present

No offset: ideal phase plot (flat) →

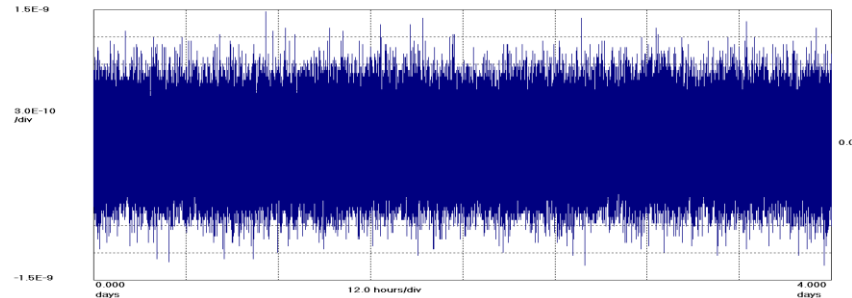


We can reduce a phase ramp to a single frequency value

# Approaches to Frequency Calculation



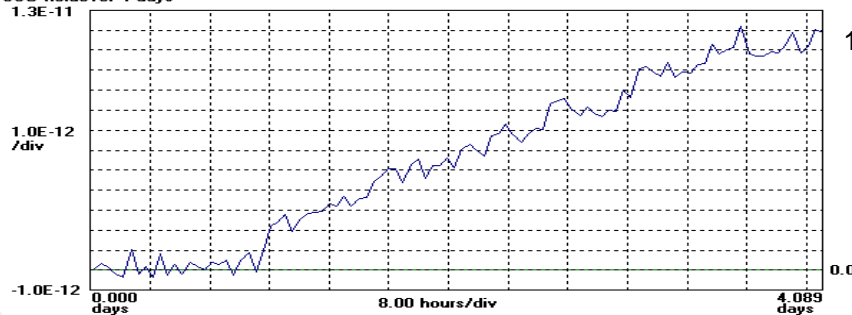
Symmetricom TimeMonitor Analyzer  
Fractional frequency offset:  $F_s=740.7$  mHz;  $F_o=2.048$  MHz; 08/15/98:07:55:45  
Holdover after 24 hours



$1.5 \times 10^{-9}$

Point-by-point

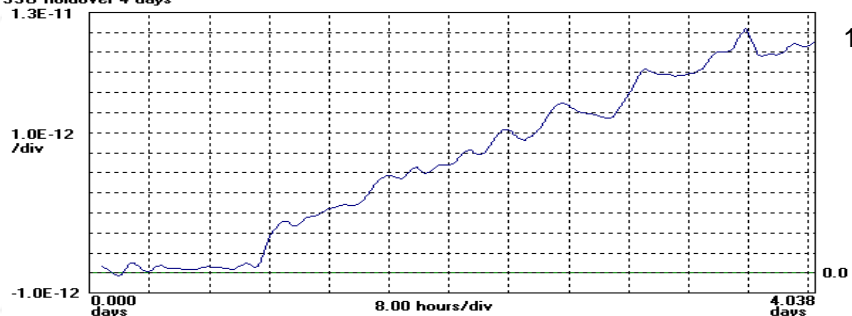
Symmetricom TimeMonitor Analyzer (file=demo\_holdover.pan)  
Least square fit fractional frequency offset vs. time; N=100; 17/18/07: 19:44:26  
SSU holdover 4 days



$1.2 \times 10^{-11}$

Segmented LSF

Symmetricom TimeMonitor Analyzer (file=demo\_holdover.pan)  
Fractional frequency offset; Overlap phase averaging; A=200; N=11056;  $F_s=32.26$  mHz;  $F_o=2.048$  MHz; 17/18/07: 19:44:26  
SSU holdover 4 days



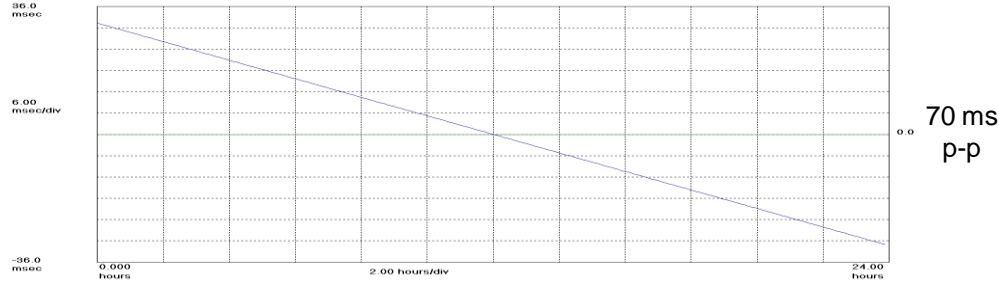
$1.2 \times 10^{-11}$

Sliding Window Averaging

# Frequency Offset and Drift

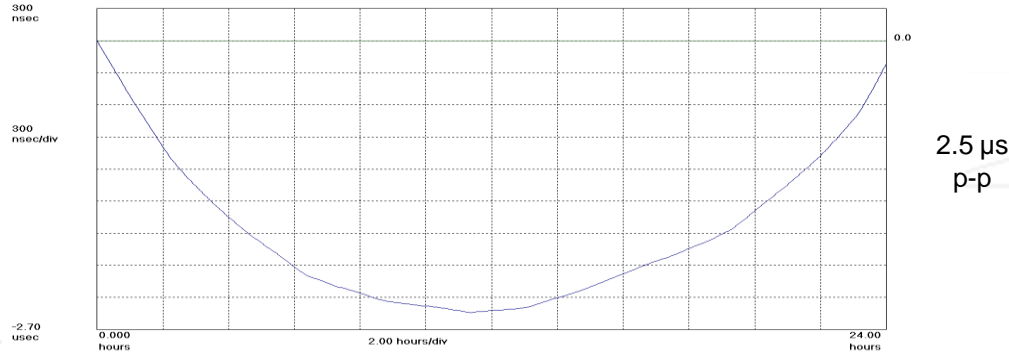


Symmetricom TimeMonitor Analyzer  
Phase deviation in units of time. Fs=296.3 mHz; Fo=10.000000 MHz; 03/12/97.02:37.24  
Test #1423, set 97.75, #23. Fo offset = -7.256E-7. Fo reference = 10.000000000000 MHz



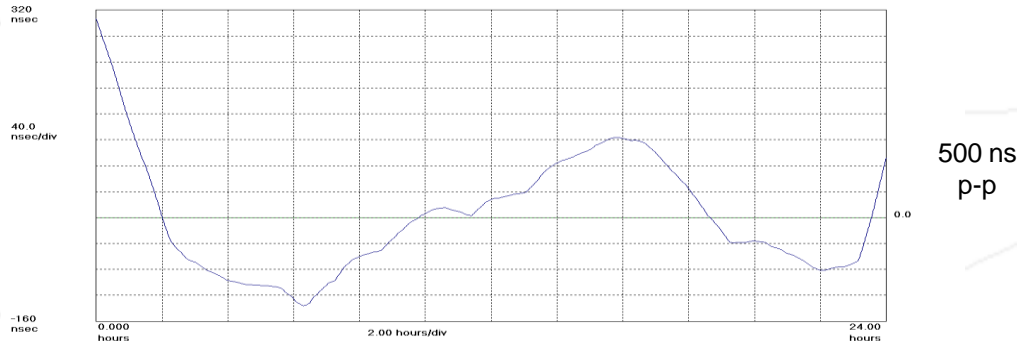
Original oscillator phase measurement (0.7ppm frequency offset)

Symmetricom TimeMonitor Analyzer  
Phase deviation in units of time. Fs=296.3 mHz; Fo=9.9999927 MHz; 03/12/97.02:37.24  
Test #1423, set 97.75, #23. Frequency Drift Rate = 2.078 mHz/day; 2.078E-10/day.



Frequency offset removed (quadratic shape shows linear frequency drift of 0.2 ppb/day)

Symmetricom TimeMonitor Analyzer  
Phase deviation in units of time. Fs=296.3 mHz; Fo=9.9999927 MHz; 03/12/97.02:37.24  
Test #1423, set 97.75, #23. Frequency Drift Rate = 2.078 mHz/day; 2.078E-10/day.



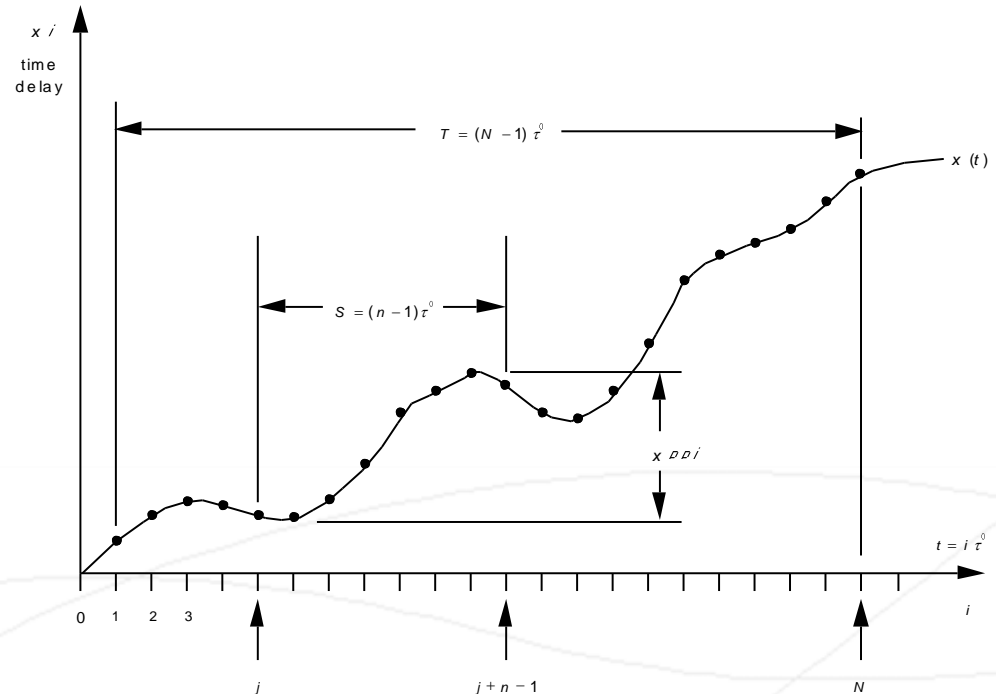
Frequency drift removed (shows residual phase movement)

# Analysis from Phase: MTIE/TDEV



$$MTIE(S) = \max_{j=1}^{N-n+1} \left[ \max_{i=j}^{n+j-1} (x_i) - \min_{i=j}^{n+j-1} (x_i) \right]$$

MTIE is a peak detector  
MTIE detects frequency offset



$$\sigma_x(\tau) = TDEV(\tau) = \sqrt{\frac{1}{6} \left\langle \left[ \frac{1}{n} \sum_{i=1}^n x_{i+2n} - 2 \frac{1}{n} \sum_{i=1}^n x_{i+n} + \frac{1}{n} \sum_{i=1}^n x_i \right]^2 \right\rangle}$$

TDEV is a highly averaged “rms” type of calculation  
TDEV shows white, flicker, random walk noise processes  
TDEV does not show frequency offset

- ▶ For traditional synchronization measurements, the measurement analysis used primarily is:
    - Phase (TIE)
    - Frequency (fractional frequency offset)
    - Frequency accuracy
    - MTIE
    - TDEV
- } All are derived from phase
- 
- ▶ MTIE and TDEV analysis shows comparison to ANSI, Telcordia/Bellcore, ETSI, & ITU-T requirements



- ▶ For packet synchronization measurements, some of the measurement analysis used is:
    - Phase (PDV)
    - Histogram/PDF\* & Statistics
    - Running Statistics
    - MATIE/MAFE
    - TDEV/minTDEV/bandTDEV
    - Two-way metrics such as minTDISP
- } Derived from PDV phase
- 
- ▶ minTDEV is under study at the ITU-T Q13/SG15 and has references in the latest G.8261 draft

\* PDF = probability density function

## Packet Delay Sequence

```
R,00162; 1223305830.478035356; 1223305830.474701511
F,00167; 1223305830.488078908; 1223305830.490552012
R,00163; 1223305830.492882604; 1223305830.489969511
F,00168; 1223305830.503473436; 1223305830.505803244
R,00164; 1223305830.508647148; 1223305830.505821031
F,00169; 1223305830.519029300; 1223305830.521302172
R,00165; 1223305830.524413852; 1223305830.521446071
F,00170; 1223305830.534542972; 1223305830.536801164
R,00166; 1223305830.540181132; 1223305830.537115991
F,00171; 1223305830.550229692; 1223305830.552551628
```

Packet  
Timestamps

Forward

#Start: 2009/10/06 15:10:30

|         |          |
|---------|----------|
| 0.0000, | 2.473E-3 |
| 0.0155, | 2.330E-3 |
| 0.0312, | 2.273E-3 |
| 0.0467, | 2.258E-3 |
| 0.0623, | 2.322E-3 |

Reverse

#Start: 2009/10/06 15:10:30

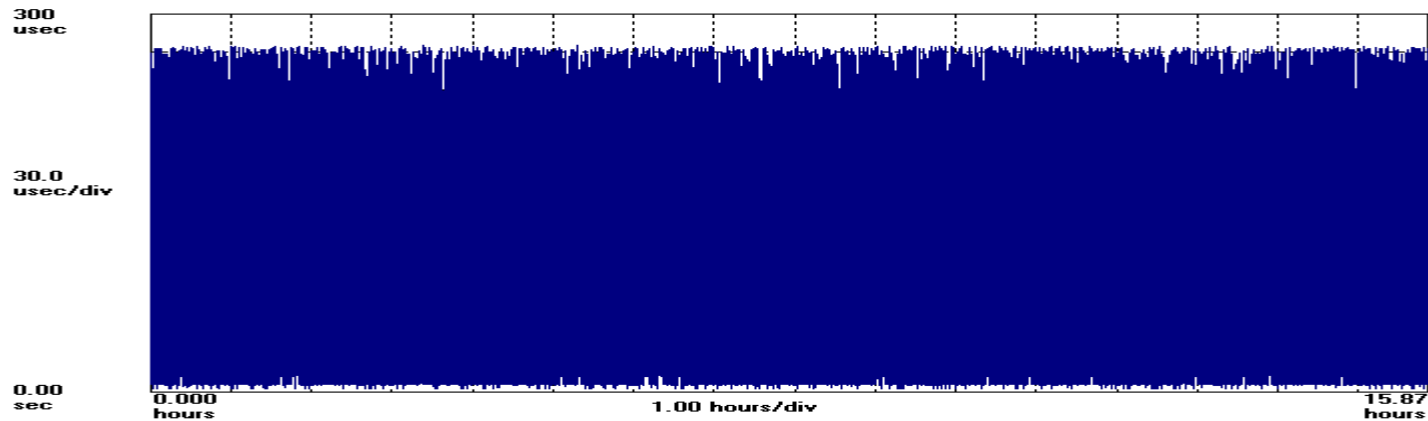
|         |          |
|---------|----------|
| 0.0000, | 3.334E-3 |
| 0.0153, | 2.913E-3 |
| 0.0311, | 2.826E-3 |
| 0.0467, | 2.968E-3 |
| 0.0624, | 3.065E-3 |

# Packet Delay Sequence



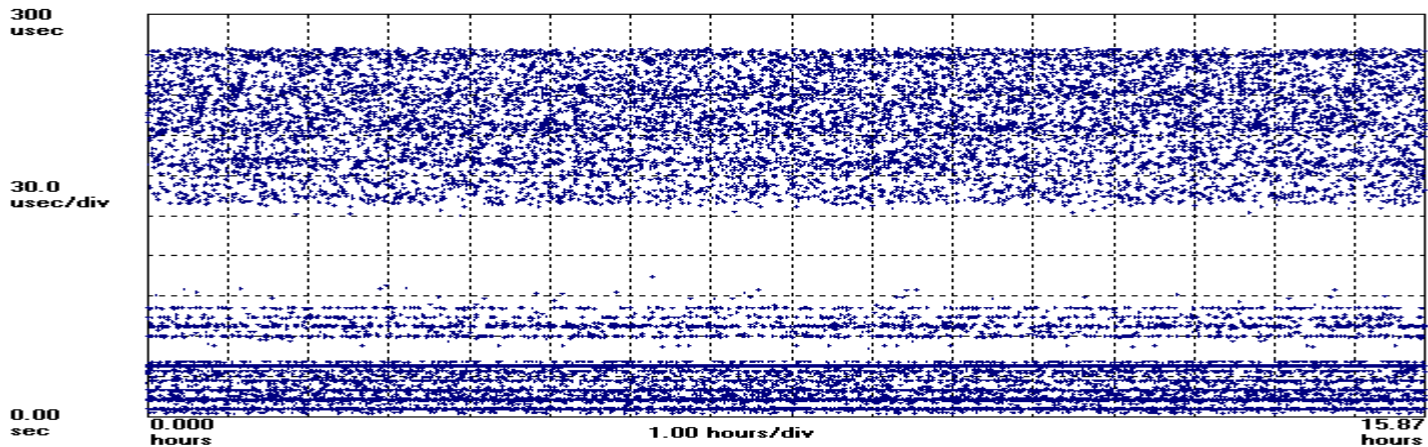
When graphing packet delay phase it is often best not to connect the dots

Symmetricom TimeMonitor Analyzer (file=xli\_1588\_pdv.tah)  
Phase deviation in units of time: Fs=500.0 mHz; Fo=10.000000 MHz; 2006/06/09 01:11:06  
XLI 1588 PDV Phase; Samples: 28561; UUID: 000055010016; Initial phase offset: 12.5420 usec



Measurement  
points  
connected

Symmetricom TimeMonitor Analyzer (file=xli\_1588\_pdv.tah)  
Phase deviation in units of time: Fs=500.0 mHz; Fo=10.000000 MHz; 2006/06/09 01:11:06  
XLI 1588 PDV Phase; Samples: 28561; UUID: 000055010016; Initial phase offset: 12.5420 usec



Measurement  
points as  
discrete dots

# Packet Delay Distribution

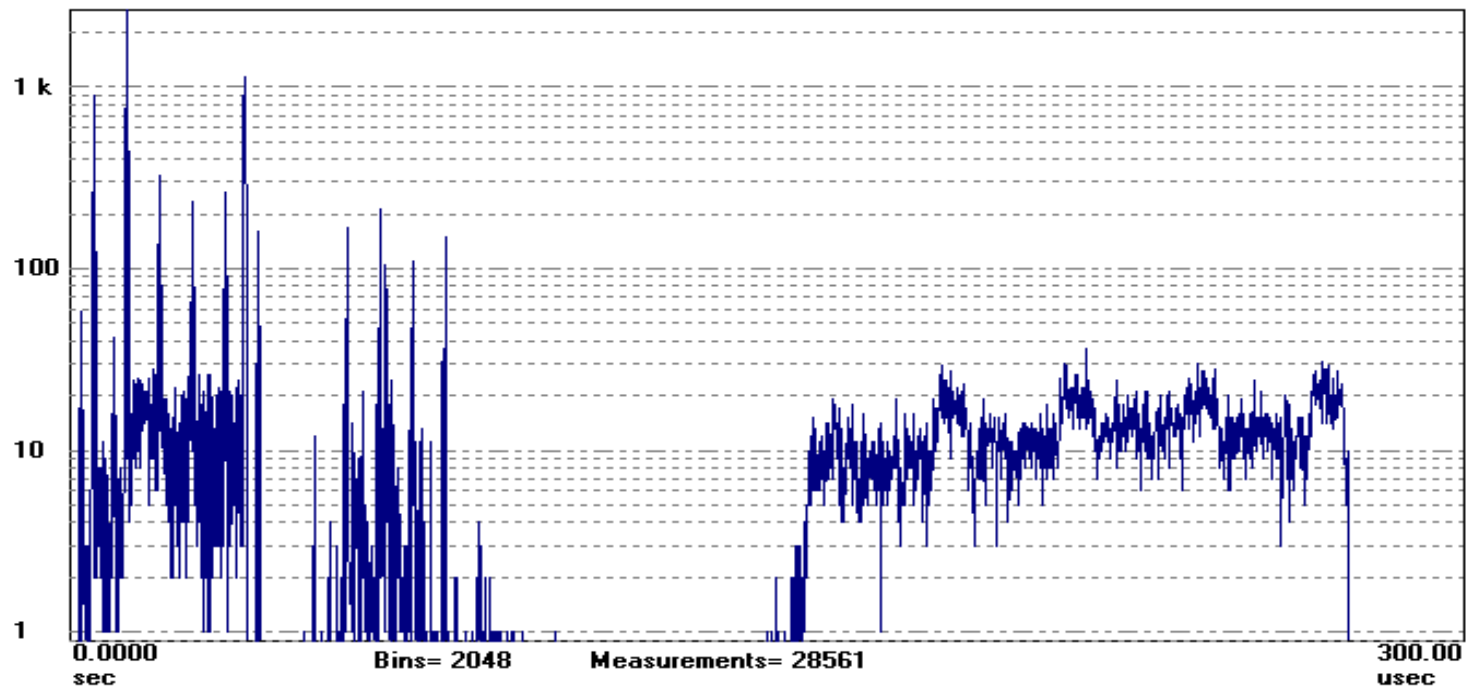


## Packet Delay Distribution

Symmetricom TimeMonitor Analyzer

Phase Deviation Histogram; Fs=500.0 mHz; Fo=10.00 MHz; 2006/06/09 01:11:06

Tahiti Phase; Samples: 28561; UUID: 000055010016; Initial phase offset: 12.5420 usec



Minimum: 1.904297 usec

Maximum: 275.2441 usec

Peak to Peak: 273.3 usec

Mean: 96.71927 usec

Standard Deviation: 97.34 usec

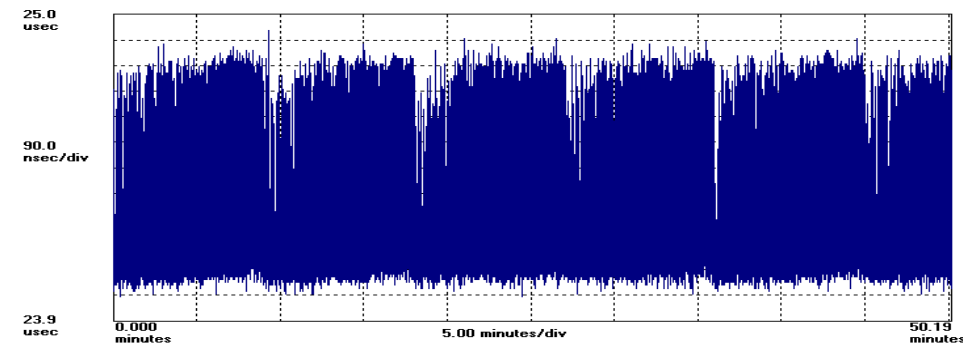
Population: 28561

Percentage: 100.0%

# Tracked Packet Delay Statistics

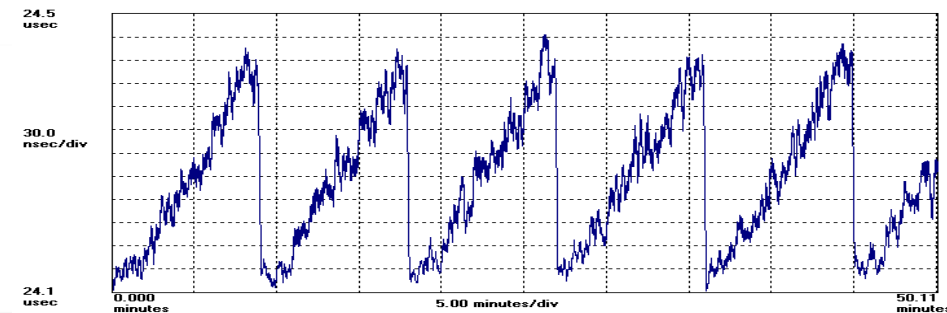


Symmetricom TimeMonitor Analyzer (file=destination-2007\_09\_19-09\_39.cap)  
Phase deviation in units of time: Fs=16.66 Hz; Fo=10.000000 MHz; 2007/09/19 07:45:00  
XLi 1588 PDV Phase; Samples: 50185; Start: 5114; Threshold: 27.0000 us; UUID: 00A069012F09; Initial phase offset: 24.1950 usec



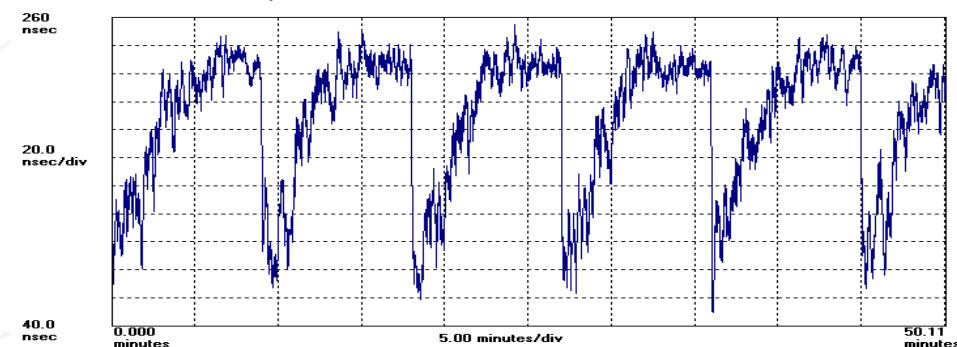
Raw packet delay appears relatively static over time

Symmetricom TimeMonitor Analyzer (file=pdv-2007\_09\_19-09\_39\_mean.pan)  
Phase Mean; Overlap: Tau=10s; A=167; N=50019; Fs=16.66 Hz; Fo=10.000000 MHz; 2007/09/19 07:45:00



Mean vs. time shows cyclical ramping more clearly

Symmetricom TimeMonitor Analyzer (file=pdv-2007\_09\_19-09\_39\_stddev.pan)  
Phase Standard Deviation; Overlap: Tau=10s; A=167; N=50019; Fs=16.66 Hz; Fo=10.000000 MHz; 2007/09/19 07:45:00



Standard deviation vs. time shows a quick ramp up to a flat peak

**MATIE**      
$$MATIE(n\tau_0) \cong \max_{1 \leq k \leq N-2n+1} \frac{1}{n} \left| \sum_{i=k}^{n+k-1} (x_{i+n} - x_i) \right|, \quad n = 1, 2, \dots, \text{integer part } (N/2)$$

**MAFE**      
$$MAFE(n\tau_0) = \frac{MATIE(n\tau_0)}{n\tau_0}$$

Reference: *Maximum Average Time Interval Error*, WD 60, Nokia-Siemens Networks, ITU-T Q13/15, Rome, Sep. 2008.

## TDEV

$$\sigma_x(\tau) = TDEV(\tau) = \sqrt{\frac{1}{6} \left\langle \left[ \frac{1}{n} \sum_{i=1}^n x_{i+2n} - 2 \frac{1}{n} \sum_{i=1}^n x_{i+n} + \frac{1}{n} \sum_{i=1}^n x_i \right]^2 \right\rangle}$$

## minTDEV

$$\sigma_{x\_min}(\tau) = \min TDEV(\tau) = \sqrt{\frac{1}{6} \left\langle [x_{min}(i+2n) - 2x_{min}(i+n) + x_{min}(i)]^2 \right\rangle} \quad x_{min}(i) = \min [x_j] \text{ for } (i \leq j \leq i+n-1)$$

## bandTDEV

$$\sigma_{x\_band}(\tau) = bandTDEV(\tau) = \sqrt{\frac{1}{6} \left\langle [x'_{band\_mean}(i+2n) - 2x'_{band\_mean}(i+n) + x'_{band\_mean}(i)]^2 \right\rangle} \quad x'_{band\_mean}(i) = \frac{1}{m} \sum_{j=a}^b x'_{j+i}$$

To define bandTDEV, it is first necessary to represent the sorted phase data. Let “x ´” represent this sorted phase sequence from minimum to maximum over the range  $i \leq j \leq i+n-1$ . Next it is necessary to represent the indices which are themselves set based on the selection of two percentile levels. Let “a” and “b” represent indices for the two selected percentile levels. The averaging is then applied to the “x ´” variable indexed by “a” and “b”. The number of averaged points “m” is related to “a” and “b”:  $m=b-a+1$ .

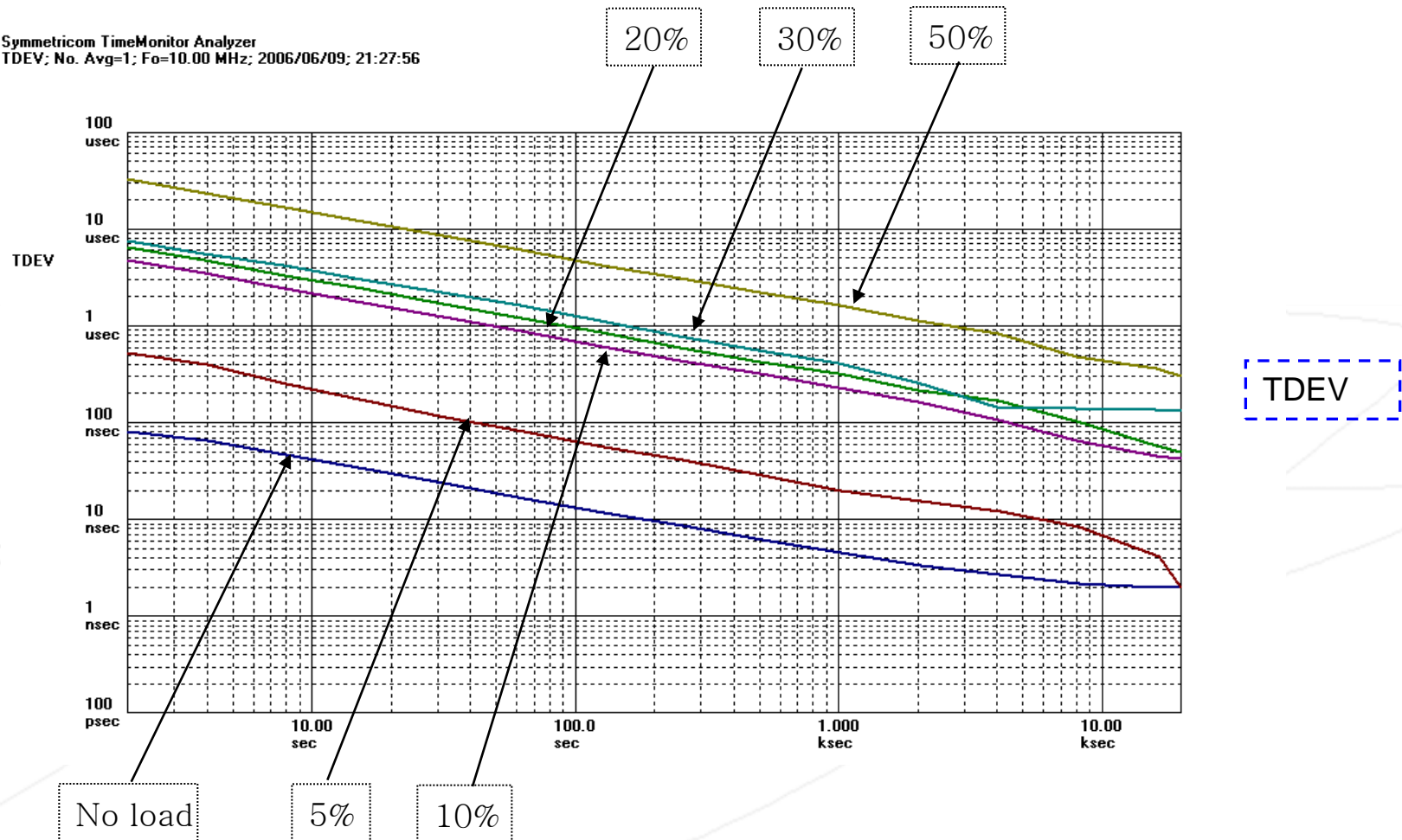
1. TDEV is bandTDEV(0.0 to 1.0)
2. minTDEV is bandTDEV(0.0 to 0.0)
3. percentileTDEV is bandTDEV(0.0 to B) with B between 0.0 and 1.0

References: *Definition of Minimum TDEV (minTDEV)*, WD 27, ITU-T Q13/15, Geneva, June 2007  
*Definition of BandTDEV*, Symmetricom, WD 68, ITU-T Q13/15, Rome, Sep. 2008.

# TDEV with Traffic



Symmetricom TimeMonitor Analyzer  
TDEV; No. Avg=1; Fo=10.00 MHz; 2006/06/09; 21:27:56



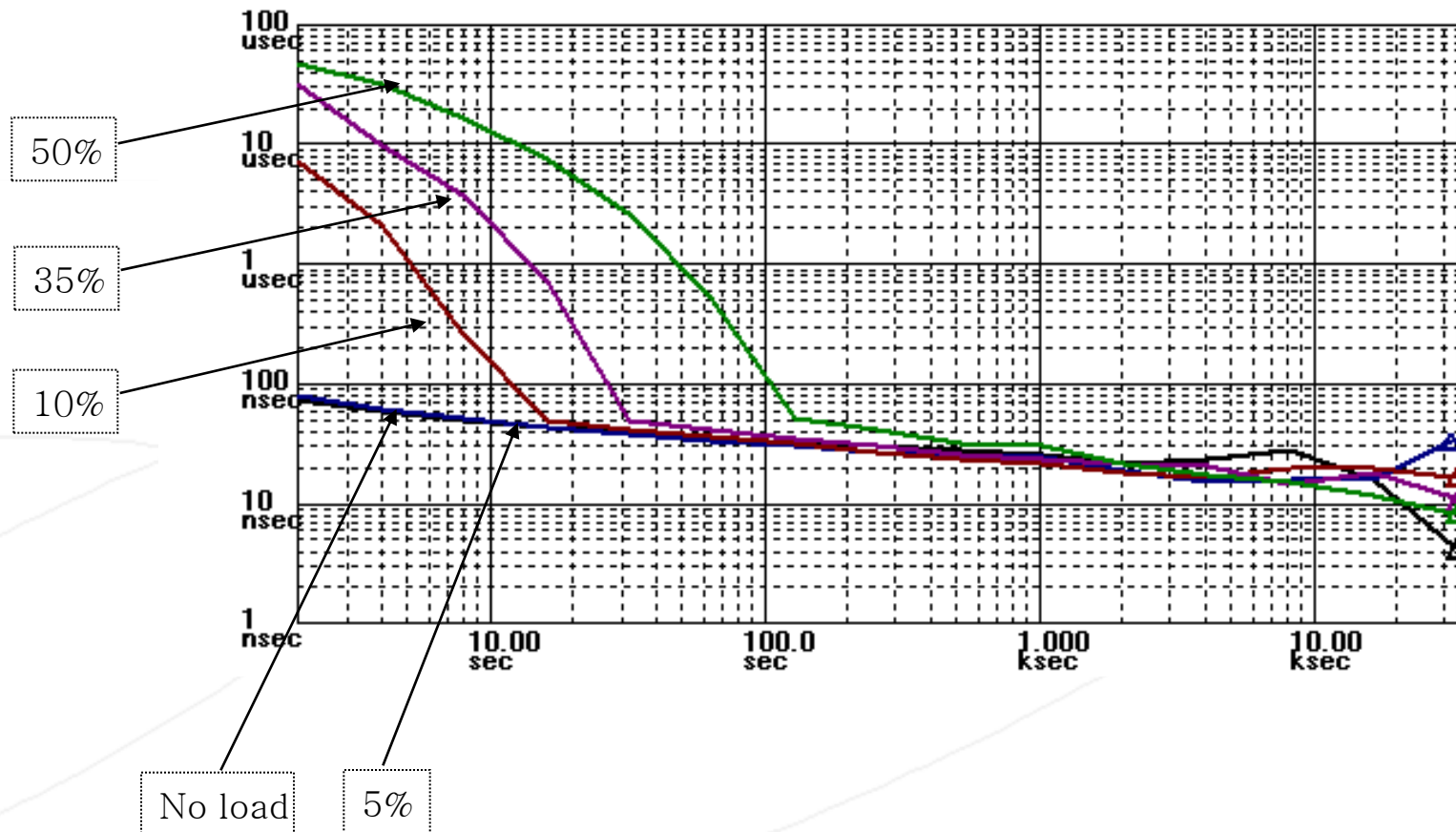


# minTDEV with Traffic



Lower levels of noise with the application of a MINIMUM selection algorithm  
TDEV at various traffic levels on a switch (0% to 50%) converge

Symmetricom TimeMonitor Analyzer (file=multilayer\_switch\_40percentSB60.txt)  
minTDEV; No. Avg=1; Fo=10.00 MHz; 2006/09/19; 15:28:30

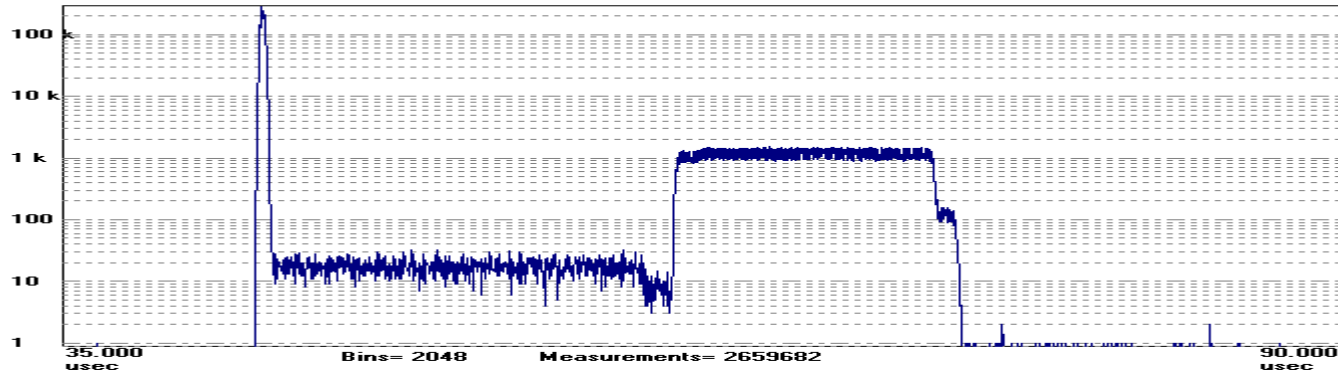


# Loaded Multilayer Switch: TDEV and minTDEV

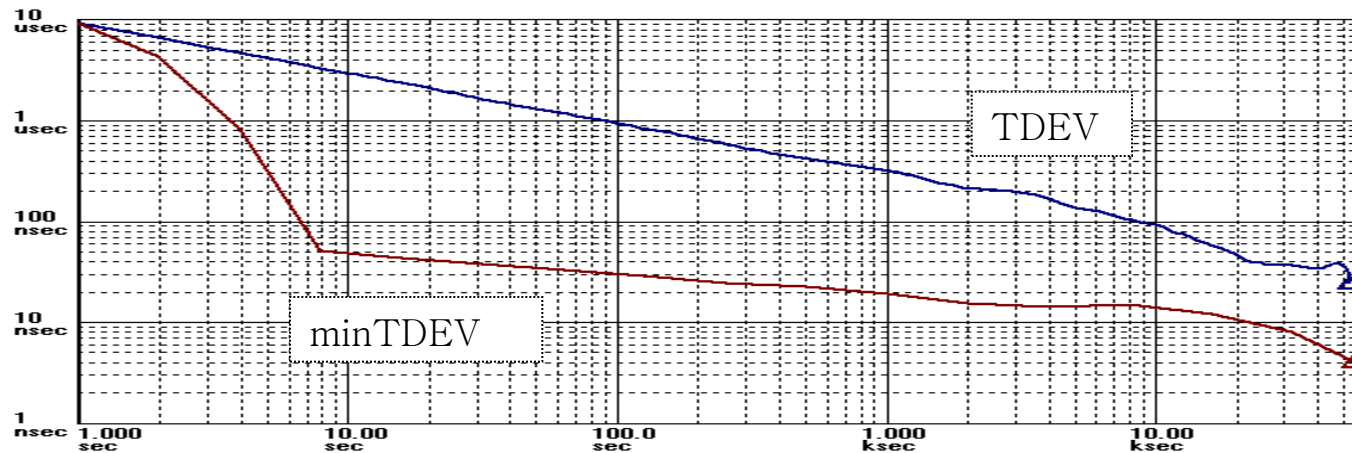


Mean: 48.3  $\mu$ sec / Peak to Peak: 50.9  $\mu$ sec / Standard Deviation: 9.43  $\mu$ sec

Symmetricom TimeMonitor Analyzer  
Phase Deviation Histogram: Fs=16.31 Hz; Fo=10.00 MHz; 2006/10/09 20:59:40  
XLi 1588 PDV Phase: Samples: 2659682; UUID: 00A069012FBA; Initial phase offset: 71.7970 usec



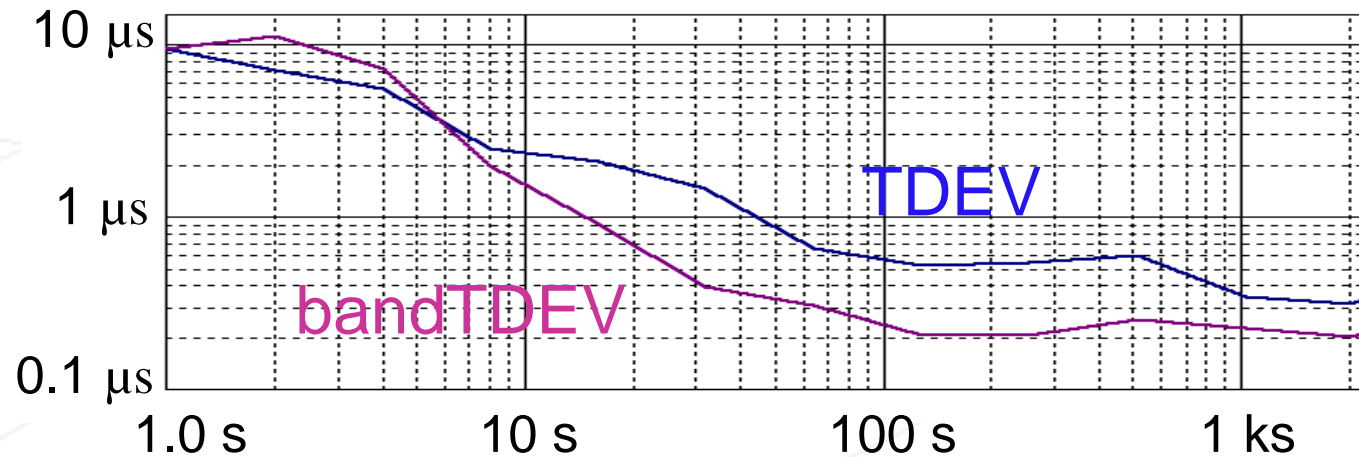
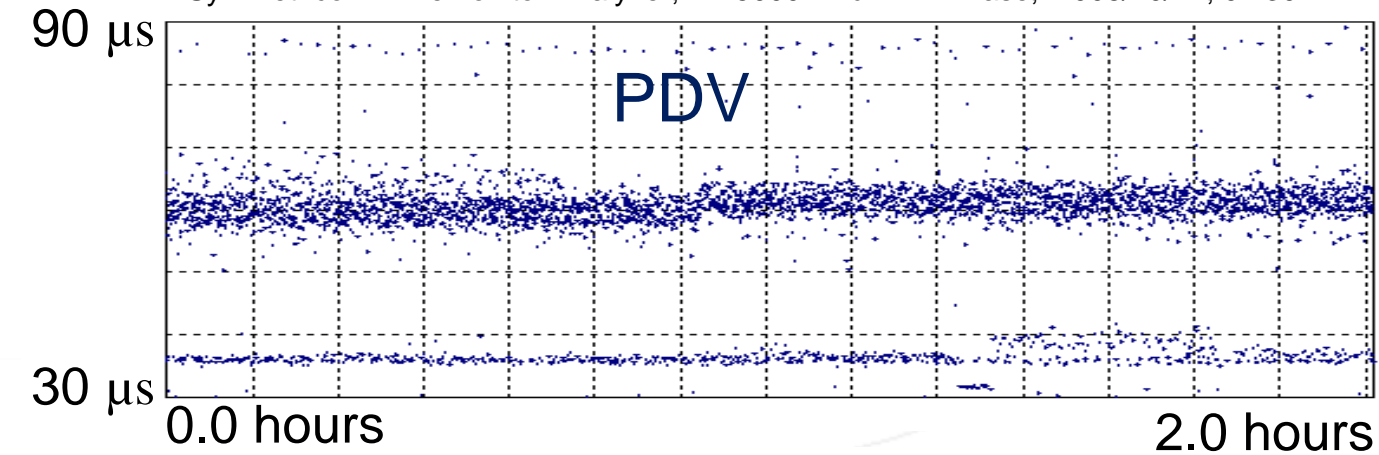
Symmetricom TimeMonitor Analyzer  
TDEV: No. Avg=1; Fo=10.00 MHz; 2006/10/09; 20:59:40  
1 (blue): TDEV; 2 (red): minTDEV



# bandTDEV Calculation



Symmetricom TimeMonitor Analyzer; TP5000 Fwd PDV Phase; 2008/10/17; 01:30:27



## Two-way Data Set

### Forward Packet Delay Sequence


#Start: 2009/10/06 15:10:30

|         |          |
|---------|----------|
| 0.0000, | 2.473E-3 |
| 0.0155, | 2.330E-3 |
| 0.0312, | 2.273E-3 |
| 0.0467, | 2.258E-3 |
| 0.0623, | 2.322E-3 |

### Reverse Packet Delay Sequence

#Start: 2009/10/06 15:10:30

|         |          |
|---------|----------|
| 0.0000, | 3.334E-3 |
| 0.0153, | 2.913E-3 |
| 0.0311, | 2.826E-3 |
| 0.0467, | 2.968E-3 |
| 0.0624, | 3.065E-3 |



|                             |           |          |
|-----------------------------|-----------|----------|
| #Start: 2009/10/06 15:10:30 |           |          |
| 0.0000,                     | 2.473E-3, | 3.334E-3 |
| 0.0155,                     | 2.330E-3, | 2.913E-3 |
| 0.0312,                     | 2.273E-3, | 2.826E-3 |
| 0.0467,                     | 2.258E-3, | 2.968E-3 |
| 0.0623,                     | 2.322E-3, | 3.065E-3 |

Two-way  
Data Set

## Minimum Search Sequences

Constructing  $f'$  and  $r'$  from  $f$  and  $r$  with a 3-sample time window

| Time(s) | $f(\mu s)$ | $r(\mu s)$ | $f'(\mu s)$ | $r'(\mu s)$ |
|---------|------------|------------|-------------|-------------|
| 0.0     | 1.47       | 1.11       |             |             |
| 0.1     | 1.54       | 1.09       | 1.23        | 1.09        |
| 0.2     | 1.23       | 1.12       |             |             |
| 0.3     | 1.40       | 1.13       |             |             |
| 0.4     | 1.47       | 1.22       | 1.40        | 1.05        |
| 0.5     | 1.51       | 1.05       |             |             |

## Packet Time Transport Metrics

*Normalized roundtrip:*  $r(n) = \left(\frac{1}{2}\right) \cdot [F(n) + R(n)]$

*Normalized offset:*  $\eta_2(n) = \left(\frac{1}{2}\right) \cdot [F(n) - R(n)]$

*minRoundtrip:*  $r'(n) = \left(\frac{1}{2}\right) \cdot [F'(n) + R'(n)]$

*minOffset:*  $\eta_2'(n) = \left(\frac{1}{2}\right) \cdot [F'(n) - R'(n)]$

*minTDISP (minimum time dispersion):* minOffset {y} plotted against minRoundtrip {x} as a scatter plot

*minOffset statistics:* minOffset statistic such as mean, standard deviation, or 95 percentile plotted as a function of time window tau

# Metrics: Time Transport

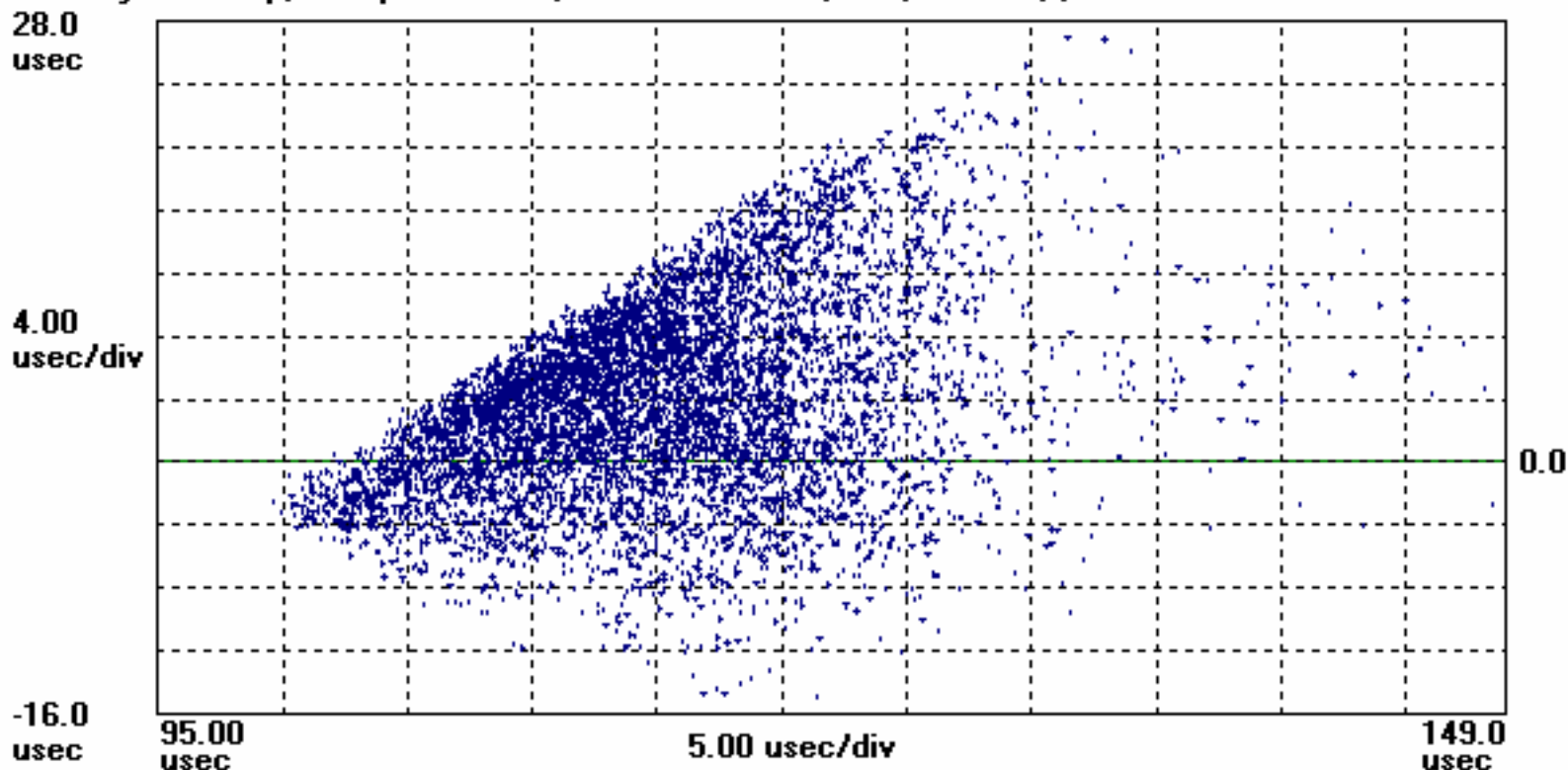


## minTDISP (minOffset vs. minRoundtrip)

Symmetricom TimeMonitor Analyzer (file=probe-2008\_09\_04--12\_54d\_fix.twy)

XY scatter plot in units of time; 2008/09/04 16:55:05

Two-Way minTDISP; Samples: 32911; Tau=993.791 ms; A=5; N=6582; ; MasterUUID: 00B0AEFFFF013183; M



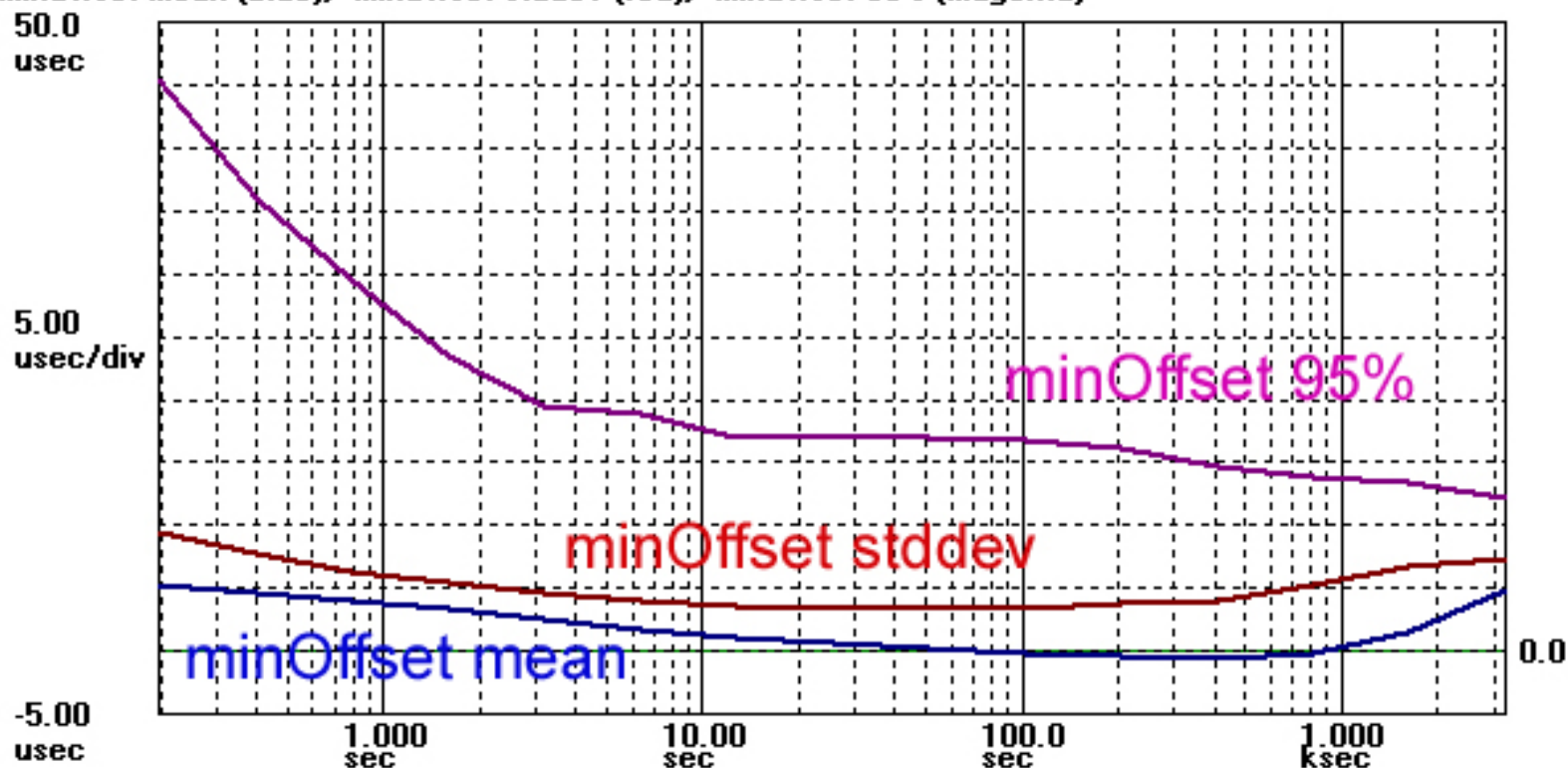
## minOffset Statistics

(Two-way minimum offset statistics vs.  $\tau$ )

Symmetricom TimeMonitor Analyzer

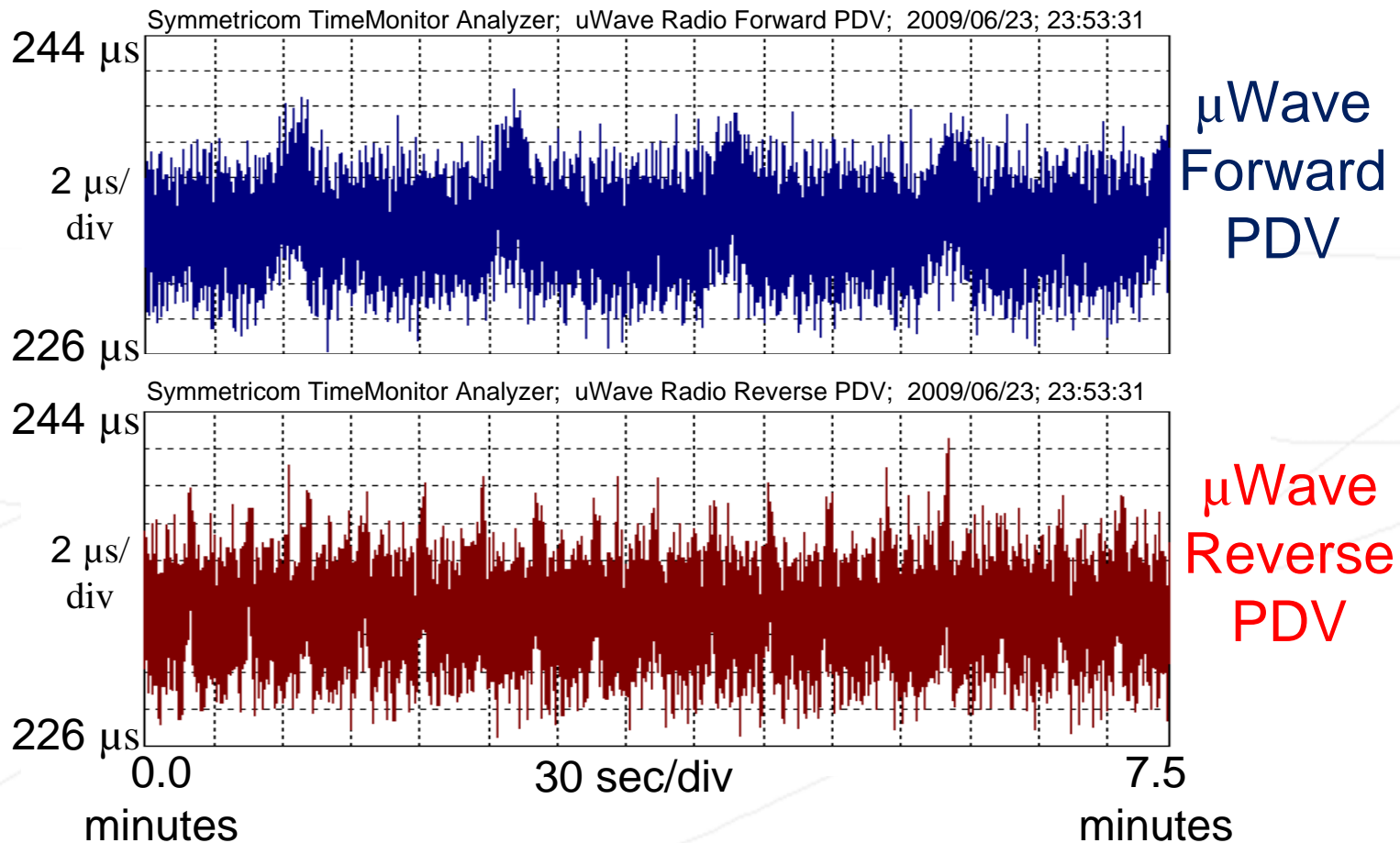
Time stats plot in units of time; 2008/09/04; 16:55:05

minOffset mean (blue); minOffset stddev (red); minOffset 95% (magenta)



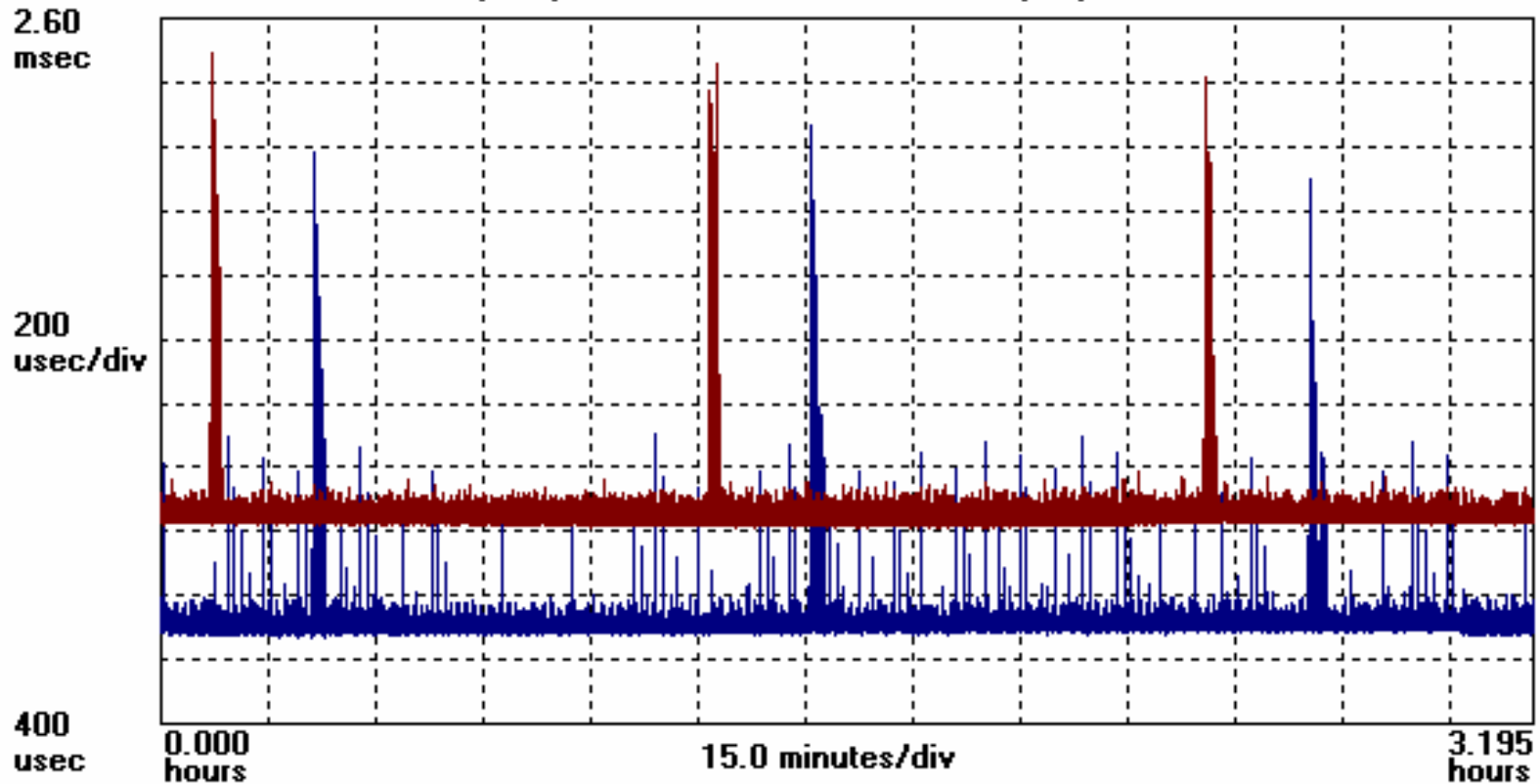


## Asymmetry in Microwave Transport (Ethernet microwave radio packet delay pattern asymmetry)



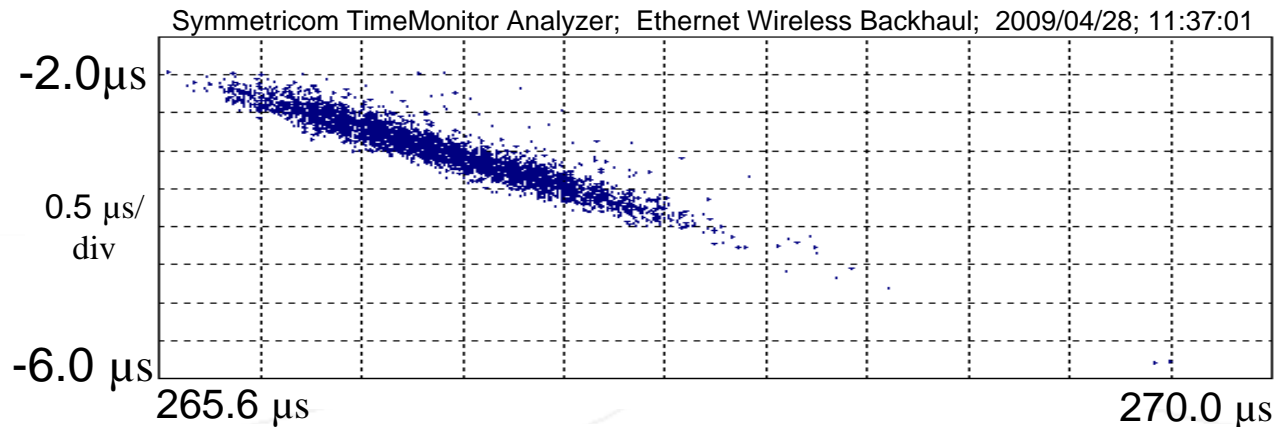
## Asymmetry in SHDSL (SHDSL forward/reverse packet delay asymmetry)

Symmetricom TimeMonitor Analyzer (file=probe-2009\_06\_16--10\_21.tpk)  
Phase deviation in units of time;  $F_s=16.00$  Hz;  $F_o=10.000000$  MHz; 2008/06/16; 09:57:27  
SHDSL DSLAM and modem; 1 (blue): TP5000 Fwd PDV Phase; 2 (red): TP5000 Rev PDV Phase

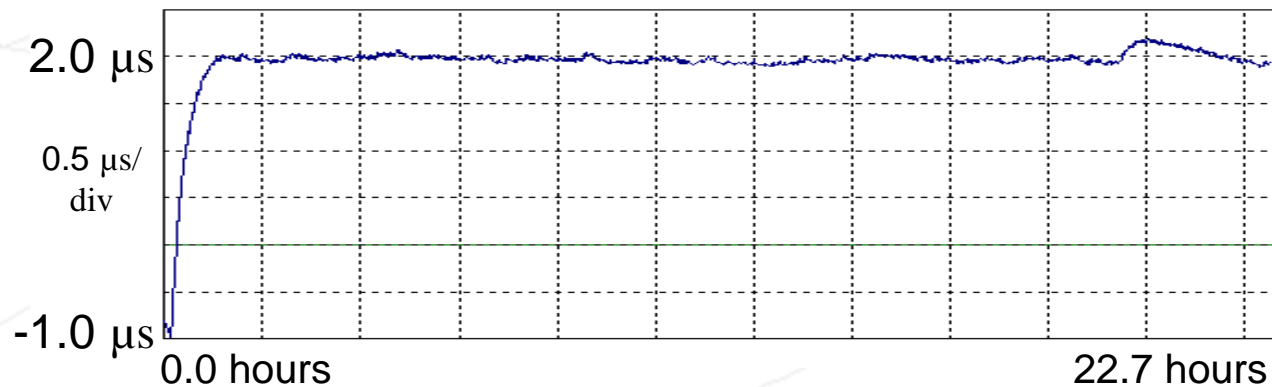


## Asymmetry in Wireless Backhaul

(Ethernet wireless backhaul asymmetry and IEEE 1588 slave 1PPS under these asymmetrical network conditions)

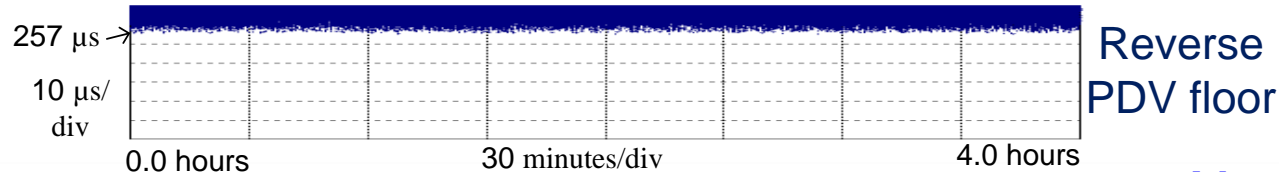
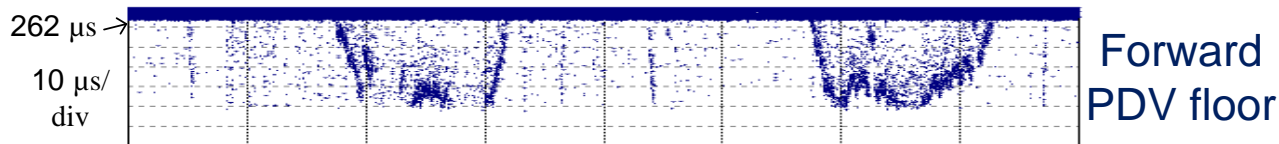


Min  
TDISP

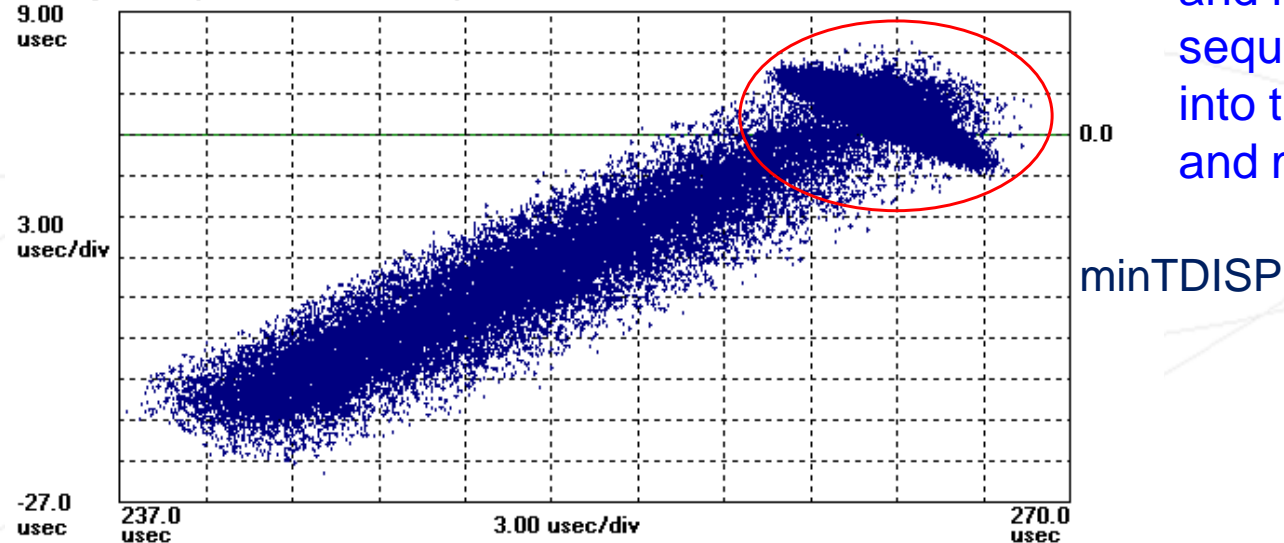


1588  
Slave  
1 PPS  
vs.GPS

## Metro Ethernet Network

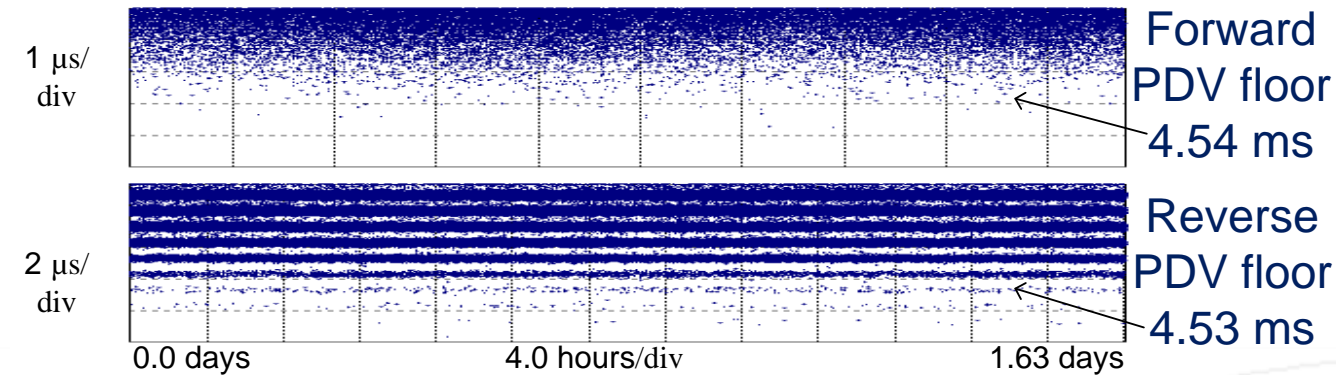


Symmetricom TimeMonitor Analyzer (file=probe-2009\_03\_05--13\_46.twy)  
XY scatter plot in units of time; 2009/03/05 18:45:33  
Two-Way minTDisp; Metro Ethernet; Samples: 1222442; Tau=999.999 ms; A=16; N=76402;

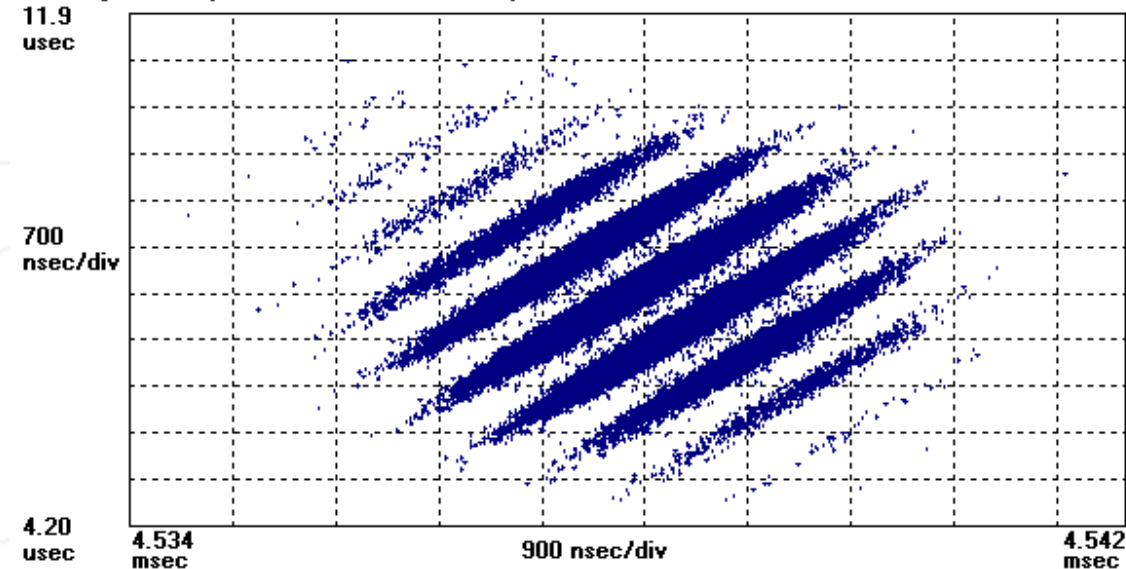


Metro Ethernet forward and reverse packet delay sequences with zooms into the respective floors and minTDISP

## National Ethernet Network



Symmetricom TimeMonitor Analyzer (file=probe-2009\_03\_30--18\_35.twy)  
XY scatter plot in units of time; 2009/03/30 16:36:32  
Two-Way minTDisp; National Ethernet; Samples: 2234610; Tau=1.00632 s; A=16; N=139663



National Ethernet forward and reverse packet delay sequences with zooms into the respective floors and minTDisp

minTDisp



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